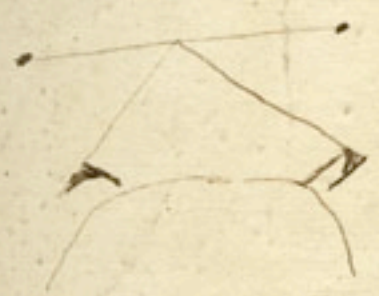


10

Prob p. 11



to answer the same purpose  
as Curvature (p. 11)

5 Jan<sup>ry</sup> 1776

I. All p. <sup>orbit</sup>  $Q^2$   $H$  and the  
 $ad = a' i = li$

II. Ellipse round the sun

III.  $p^2 = Q^3$  <sup>4</sup>  $p^1$  orbit  
whole plane  $p^1$   $H$   $ps$

The orbits are nearly ell!

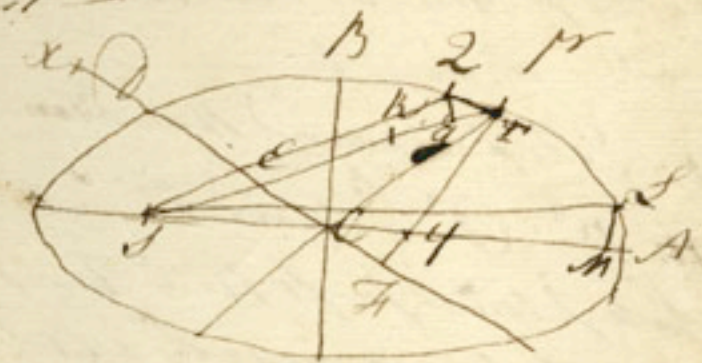
The  $p^2 = Q^3$

I. All the  $p^1$   $p^2$  are return  
in the orbits by four direct

to the sun 2.  $H$ : all the  $p^1$   
orbits are ell! having the sun

in one of the foci

The force which retains the planet  
in their orbits is inversely as the  
Dist<sup>2</sup>

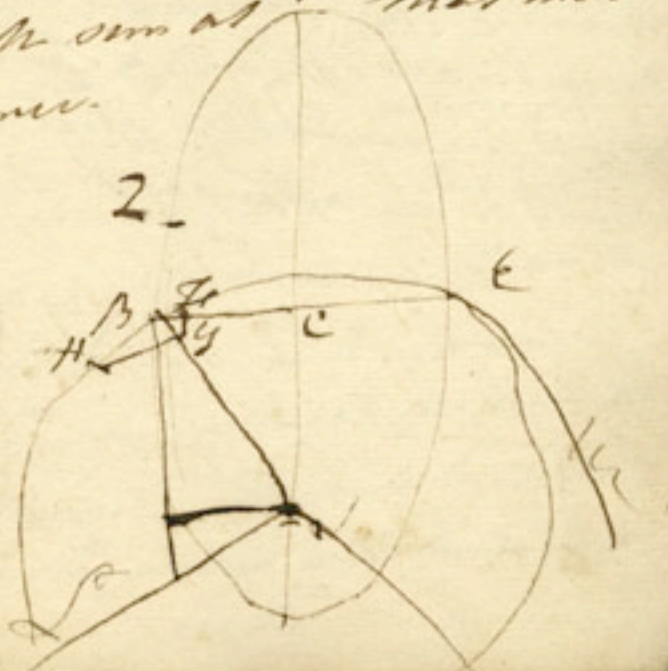


$$\begin{aligned}
 BC &: CD :: CD : CX \\
 CA &: PF :: PF : PG \\
 SA &: SP :: SP : SH \\
 2F &: LM :: VP : VA \\
 2G &: LM :: SA : SP \\
 2G^2 &: LM^2 :: SA^2 : SP^2 \\
 2G^2 &: LM^2 :: SA : SH \\
 2G^2 &: LM^2 :: CA : PF \\
 72 &: 2G^2 :: CA : PF \\
 72 &: 2G^2 :: CA : PF \\
 72 &: 2G^2 :: CA : PF \\
 72 &: LM^2 :: SA \times CA : SA \times PF \\
 72 &: LM^2 :: SA \times CA : SA \times PF \\
 V, P &: V, A :: SA \times CA : SA \times PF \\
 ch \cdot G &: P : CB :: CX : P \\
 72 &: 72 :: V, P \times CA : V, A \cdot ch \\
 72 &: 72 :: SA \times CA : SA \times PF \times CX
 \end{aligned}$$

$$\begin{aligned}
 F.P. &: P.M. :: S.A. : S.H. \\
 72 &: 72 :: S.A. : S.H. \cdot 2.E.D
 \end{aligned}$$

1<sup>st</sup> Cor.<sup>o</sup> The equation of the  
astronomy. — When the Planet  
sets out from A its direction is  
a tangent perpendicular to AB  
but at P it makes an acute  
angle and therefore its motion  
is accelerated

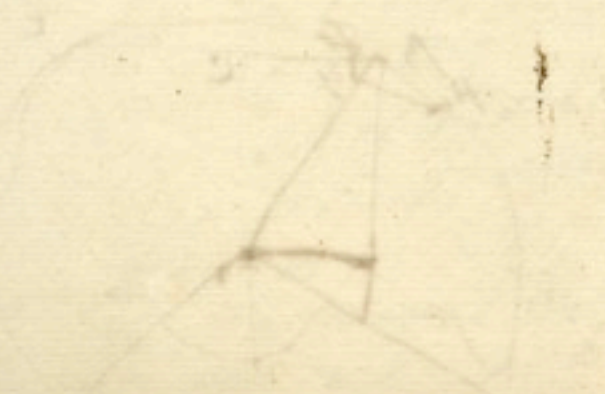
The vel<sup>ty</sup> at P is that at  
would not it were in a circle  
could be seen at that near  
Distance.



$BZ \times BE : AZ^2 : BC^2 : CA^2$   
 $BZ \times BE : BQ \times BK : BC^2 : CA^2$   
 $BZ \times BE : QH : PC^2 : CA^2$   
 $AZ^2 = QH^2 \mid QZ : PH$

This is the reason why the planet  
 does not fall into the sun  
 at the perihelion.

If the central force should de-  
 crease as the cubes of the dist.  
 increase then it may be demon-  
 strated that the planet would  
 describe an equiangular spiral  
 round the sun & the sun too  
 would never approach him.



of Jan. 1776

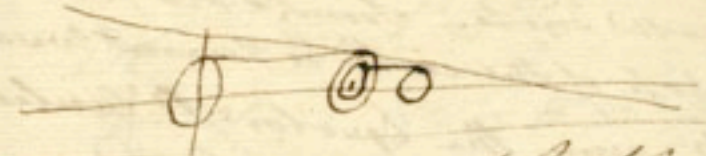
Start of the Phenomena —  
 Planets not seen — appear to us  
 by reflected light — Venus, a crescent —  
 a small ball — Annularis well exhibit  
 the same sp. with Venus or the moon.  
 Jupiter and Saturn; both same sp.  
 the eclipses of <sup>their</sup> Sat. — The  
 sun of Mars by ana? —

Eclipse of the sun or rather of the  
 earth — Penumbra — shadow  
 of the earth from left to right to  
 a spectator in the moon. breadth  
 of the shadow, & penumbra —

Eclipse of the moon — Shows the  
 earth to be round — hence we see  
 that the sun is bigger than the earth  
 and moon. — shadow of the moon of  
 different dimensions, sometimes does  
 not reach the earth.

When the moon is nearest the  
 the earth the Perseus of the line  
 is 150 miles and of the Perseus  
 hence it appears that the sun is  
 bigger the earth. More over eclipses  
 - hence also the earth is bigger than  
 the moon. - Eclipses do not happen  
 at every change in fact because the  
 moon's orbit is inclined to the plane  
 of the ecliptic - An eclipse can  
 happen unless the moon be in one  
 of the Nodes. - Moon's orbit from  
 the node of change to the next  
 is  $30^{\circ}$  + the motion of the node. Hence  
 there can be no eclipse at both  
 those times. If the Moon is in  
 the  $18^{\circ}$  from the node there will be  
 an eclipse of the sun - July 1797  
 1st of month & an eclipse of the moon  
 happened at an angle of  $5^{\circ}$

Moon's inclination

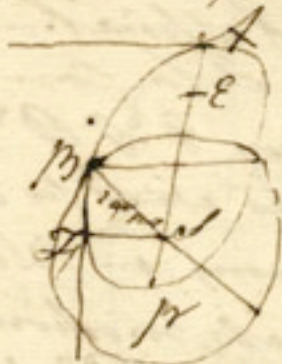


The E of Sun cannot be  $12^{\circ}$   
 unless the Sun be kept to the  
 of the Nodes. Less than the solar  
 because of the decrease of the conical  
 shadows.

A D H 49' period of eclipses -  
 variation  $\frac{1}{2}$  Degree  
 Quantity of shadow intercepted &c  
 Sun the solar limits can't longer  
 the Sun it would appear that  
 there should be an eclipse of the  
 sun the moon - this not the  
 case &c - Total eclipse of the Sun  
 of duration of a total E.  $4^{\circ} 5''$

To estimate the quantity of the  
 eclipse the diam. of the sun and moon  
 are sup<sup>d</sup> divided into 12 equal parts  
 each digit. Sun's Solo's north  
 pole of the earth is turned toward  
 the sun. the Equator P's Circles  
 will be ellipses - Eclipses  
 of the sun will appear very  
 various to a spectator, from  
 the position of the Moon, of the  
 node, and of the Spectator -  
 Ap. of an ellipse at the Sun's  
 Solstice and at the Autumnal  
 Equinox. - Lunar eclipses  
 not subject to these variety  
 seen to all other suns here.

8 Jan. 1776



It was demonstrated

$$V^2 \propto \frac{v^2}{D}$$

$$\frac{1}{D} \propto F' = \frac{v^2}{D}$$

$$\frac{1}{D} \propto v^2$$

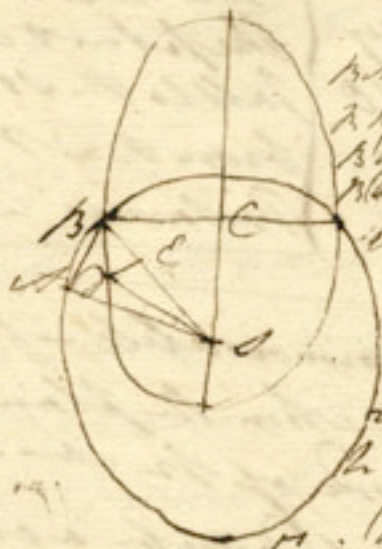
$$V^2 B : V^2 A :: S A : S B$$

Proof the Vel. at A is too  
 small to allow the planet to  
 move round the sun in a  
 circle whose radius is SA.  
 - Velocity at B is too great  
 to allow the planet to move  
 round the sun in a circle  
 whose radius is SB -  
 - Diminution on one side  
 = augmentation on the other  
 - If the solar power was in  
 as D<sup>2</sup> the planet would come

would be seen in an equat.  
 or Logarithmick spiral.

If the force of the Saturn force is  
 something between  $D^2$  &  $D^3$  the  
 line of the Apisides will be con-  
 tinually advancing in the  
 direction of planets motion -

If the Saturn force was  $D^2 + \frac{1}{2} D^3$   
 the result of the Apisides would  
 be very sensible. A March  
 has been observed, at least  
 very little and this may be  
 accounted for on other  
 principles



$AS : BS :: BA : BE$   
 $AS : BS :: BD : ED$   
 $AD : DE :: BS : BE$   
 $AD : DE :: CF : BC$   
 $AS : BS :: CF : CB$   
 $O : O :: CF : CB$

When the  
 planet is in C  
 the C.F. is  $\frac{C}{r^2}$

$$F = \frac{C}{r^2} \quad F' = \frac{1}{r^2}$$

In the planets the forces are inverse  
 $\therefore D^2$  The forces are not different  
 but the same forces acting at  
 different distances. All the  
 planets at the same dist. and  
 with the same vel.<sup>ty</sup> would  
 describe = orbits. - Hence the  
 Centripetal force is  $\therefore$  quantity of  
 matter at = distances - Hence  
 we can find in what way the  
 world should be

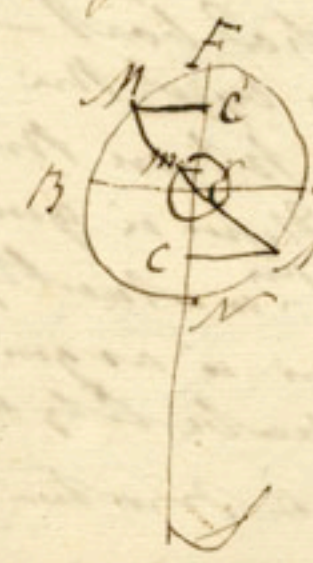
$M = 45'' \frac{1}{2}$   
 $V = 39'' 17$   
 $E = 64'' 10$   
 $M = 121''$   
 $J = 290''$   
 $S = 768$

The in which  
 the planet would  
 fall to the Sun  
 from this M.  
 Distances

Sun not immovable - found  
 by observation when the planets  
 are on one side of the Sun -  
 Sun is found to describe a curve  
 round a fixed point. This pt.  
 can explain for. by an equal  
 in their orbits by their tenden-  
 cies to each other. The apt-  
 inferences will equal with  
 when the same motions round  
 a point. - Found by Sun &  
 planets mutually equal.  
 This pair has this property.

any body has D. inverts ::  
 to the quantity of Matter:

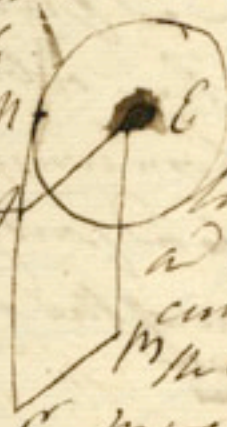
9 Jan<sup>ry</sup> 1746  
 Between the sun & Jupiter M.  
 M. E. is between their orbit - sine  
 of the Distance from conjunction  
 E. found nearer to a farther from.  
 The Sun is sine of the Distance  
 from conjunction  
 quadrature



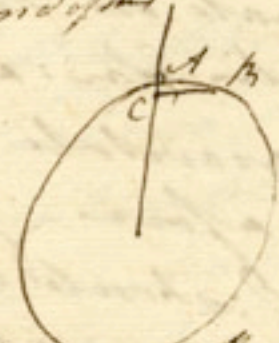
The sun's way  
 takes place betw  
 Ari J. & Sat.  
 Sometimes very  
 stable if

Then the Sun E. & M. are  
bodies regulated by the same  
Muhamed forces —

Now is act not only  
by the force tending to the C  
center by a force  
tending M. to the Sun  
supra. A boat o' sheep  
to the moon  
a boat in a  
current. maybe  
the same the Sun  
& must act equally  
both on the sheep & boat —  
Hence the forces by w<sup>ch</sup> the  
Sun & Sunday M. are the  
same in all. Hence in general  
the Sun and M. mutually  
tend to other; this is as general  
as this penetrability or  
penetrability is not



I. J. N. says wh<sup>ch</sup> the Moon  
is the same, or a new force —  
— Suppose a moon a foot E.  
revolve round the earth on its  
surface — the  
 $M^2 : m^2 :: R^3 : \frac{1}{2} D^3$  of the Earth  
how we have the greatest velocity of  
the orbits when the two Moons  
is a given time —  
Paris fall 16.054 | tell Sat. with  
in a second of the | now in 1 second  
76.054



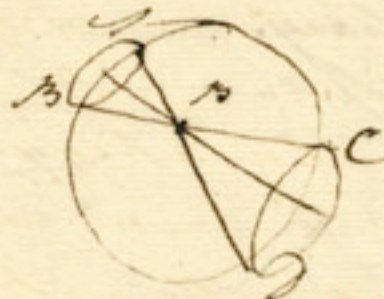
For the force of the planets is  
the same with terrestrial gravity  
I. G. or that force by which bodies  
fall on the earth is the same  
with that power which keeps I.



In this case. — Subst. G<sup>n</sup>  
 for the planetary force.

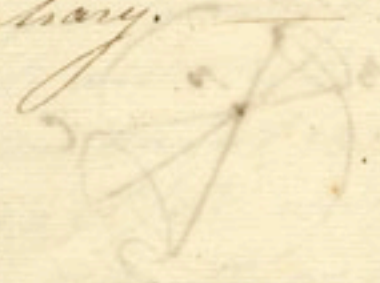
Since the gravitation of all  
 the planets are ∴ to their  
 quan.<sup>ty</sup> of matter at equal  
 Distances — I J N consider  
 the inertia of matter as the  
 proper test of the quantity  
 of matter — Indications of  
 different bodies and the same  
 lengths, vibrate in the same  
 time. *Hyacinth* in all  
 bodies ~~gravitate~~ gravitate to  
 each other with a force ∴ all  
 bodies on our E: should do the  
 same but this is not found  
 except in Magnets and Elect<sup>ric</sup>  
 and this do not ~~force~~ ∴ On If the  
 attraction did take place as

could not be observed on account of the  
 quantity of matter  
 I do not follow that the P<sup>er</sup>



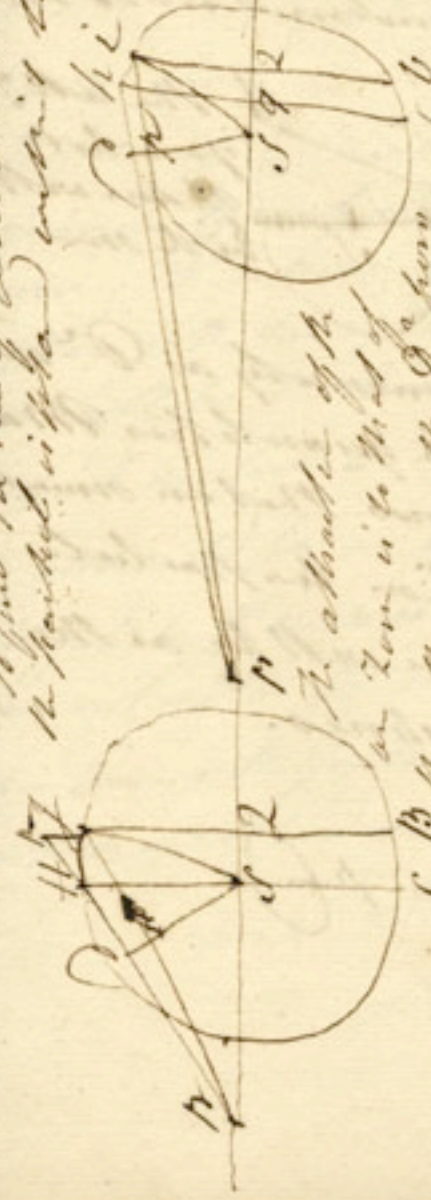
$11^2 \times 11^2$  } Hence when the  
 $11^2 \times 11^2$  } particles P or p  
 are equally attracted  
 and therefore will rest — The  
 same will happen if the Part<sup>ic</sup>  
 is enclosed in a <sup>thick</sup> shell — The  
 the whole will be uniform  
 and may be enclosed within a  
 shell to which every part P or p  
 is equally attracted. E: shell  
 Earth may have a cavity within  
 it and there may be different

Habitable Bodies in this  
cavity for ought we know  
to the contrary.



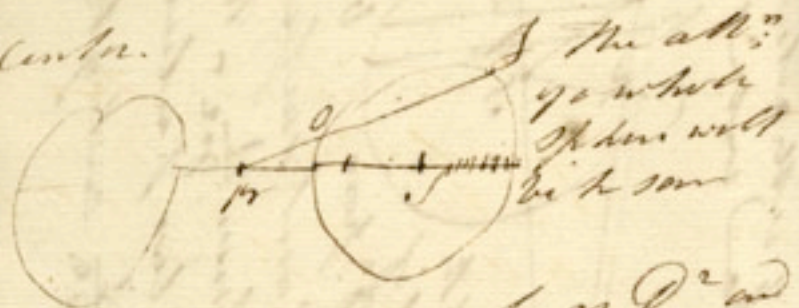
10 Jan<sup>y</sup> 1776

To find the law of attraction w<sup>ch</sup>  
the Planet will be w<sup>ch</sup> it be of the

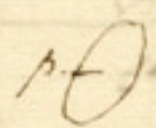
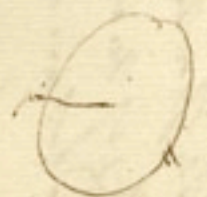


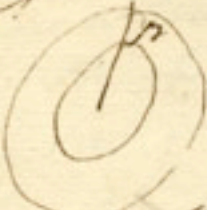
The center & Hence the whole spheroid surface will  
attract the Particles P, p with force  $\frac{1}{2}$  times a  
sp. quantity of Matter will attract two Particles at  
equal Distances with force  $\frac{1}{2}$  each of the

The sum of the attraction  
will be the same of all the  
matter was condensed into the  
center.



A. Sp. are inversely as  $D^2$  and  
directly as the quantities Mat.  
Hence it follows that in equal  
spheres the attr: on two particles  
on their surface will be as the  
radius of the spheres.

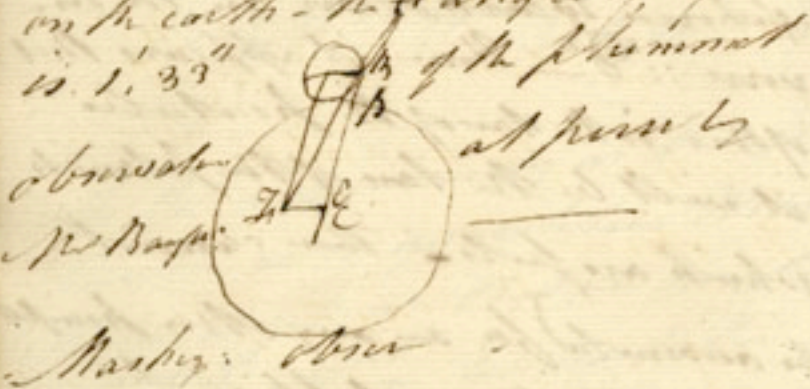


The Partic.  $P^2$  tends to the  
cent. w<sup>th</sup> a force  $C$  directly  
as  $D^2$ .  Hence the attr:

Hence the attraction of two  
spheres to each other in the in-  
verse  $\therefore D^2$ . Hence it appears that  
of this is the law of the particles  
it will be the law of the planets  
which are facts. These cannot  
be accounted for on any other principle  
except that of Newton's gravitation. It  
does not explain the cause the only  
mention of the facts.  $Q^2$  is an universal  
property of all bodies

11 Jan<sup>y</sup> 1706  
 N m  
 g<sup>2</sup>

Small globe 1 League D<sup>r</sup> low  
 on the earth - the angle of Reflexion  
 is 1' 33"



some of the low  
 Deflect in hollow amounting to  
 about 22" - each 11' side of the ball

The plummet will point to the  
 center or where except at the  
 Eq. and the poles i.e. at the  
 extremities of the two axes

Planets attract each other,  
 and consequently disturb each  
 others motion, in  $\propto \frac{2iM}{g^2}$

To find the quant. of M. in  
 the space

$$g \propto \frac{M}{D^2} \quad g \propto \frac{D}{P^2 \text{ time}}$$

$$\frac{M}{D^2} \propto \frac{D}{P^2}$$

$$M \propto \frac{D^3}{P^2}$$

$$M \propto \frac{1}{1} = 1$$

$$D \propto \text{distance of } J: \text{ to } \text{Sol.}$$

$D^3 M: m :: 1: 1067$   
 Divide the D. by the 1<sup>st</sup> in low  
 planets, then 1. quote: 2. quote as  
 the quant. M in the one is to g. M. in g.

$\rho''$   $\frac{1}{365 \frac{1}{4}}$   
 $3 \Delta 20 = d$   $27 \frac{1}{2}$  Matter in Sun.  
 E. Area  
 M: M: 1 : 965412

		Diam.
Matter	—	112.5
Sun	365412	= 11.
Jup.	340	= 10.
Sat.	107	= 1.
Earth	1	1.
Mars	$k: .425$	.4 A
Ven.	$k^n 1.171$	1.3 A
Moon	$k^n .2$	.7 k

	Density
Earth	1
Jup.	$\frac{1}{4} .23$ Sat. $1 \frac{1}{4}$
Sun	$\frac{1}{4}$

2. M<sup>2</sup> nearly as 1<sup>2</sup> of the planets

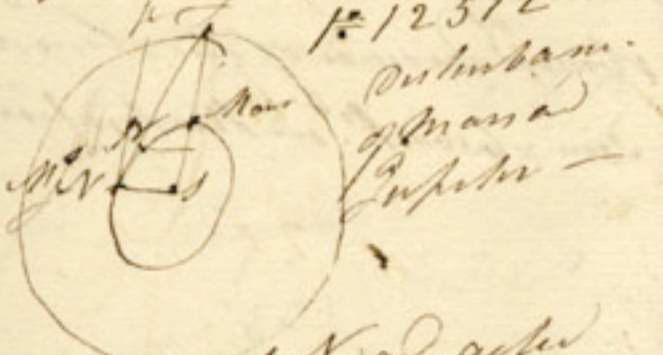
Gravity proved by the most uniform induction which Nature affords

$\frac{16.1M}{R^2}$  Feet.  
 In 478 at top of Mt. ...  
 on the surface  
 of the planets  
 Just in a  
 second

How the planets move in space  
 Moons retardation caused by  
 the resistance of the Earth's  
 atmosphere, this resistance more  
 than sufficient to account for the  
 observed decrease of the lunar month  
 Sun = 6500 f. in the system

12 Jan 9 - 1776

All the planets attract all  
the planets therefore they disturb  
each other in their motion -  
The Sun M<sup>r</sup> is the cause why  
the planets are kept in their  
than otherwise they would be -  
Sun's attraction of them by small



Jupiter was at N and acted  
upon by J<sup>r</sup> in a low part  
to J<sup>r</sup> he would not be disturbed  
the gravity of Jupiter

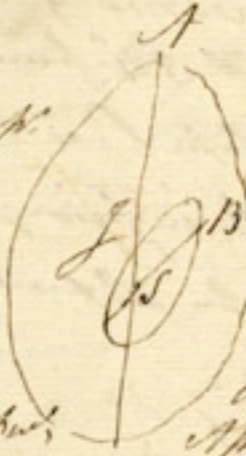
When a superior P<sup>r</sup> is in conjunction  
with a sup<sup>r</sup> is gravely to the  
Sun is diminished by v. v.  
Point P about 54° from M.  
of Efflux of P<sup>r</sup> is to Disturb  
the figure of the inferior planet  
at the time of the conjunction  
Precedence -  
Apell. of

M	0° 24' 26"	in a 100 years the Aph <sup>a</sup> advances
V	2° 46' 26"	
E	1° 29' 56"	
J	28° 26"	
M	90° 6"	
J	90° 6"	

The actions of the P<sup>r</sup> of aph<sup>a</sup>  
the cause of M<sup>r</sup> of the Aph<sup>a</sup>

Action of J<sup>r</sup> Sat greater  
upon each other than the other

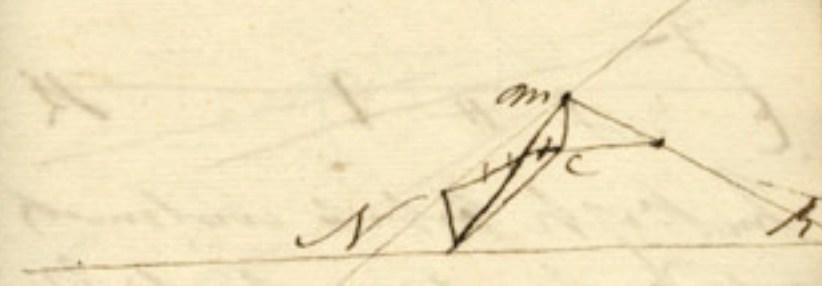
$\frac{1}{2000}$  of J<sup>r</sup>  
on Saturn  
sometimes  
the longer  
axis is  
toward backward



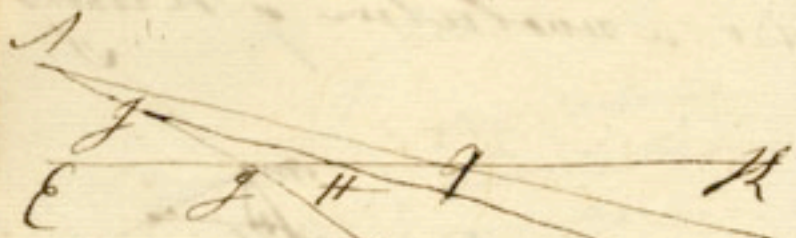
They <sup>are</sup> always  
drawn by  
Jupiter  
occasionally  
we observe  
in Saturn  
arrived at the  
Aphelion & perihelion

but in general forward.  
Attraction of a Sup<sup>r</sup> planet  
accelerates and sometimes re-  
tards the motion of an inferior -  
but these are followed in one  
revolution. Action of Sat<sup>r</sup> very  
remarkable in Jupiter's orbit.  
If all the <sup>planets</sup> J<sup>r</sup> in the same  
place then disturbance would  
be in whole but as they do

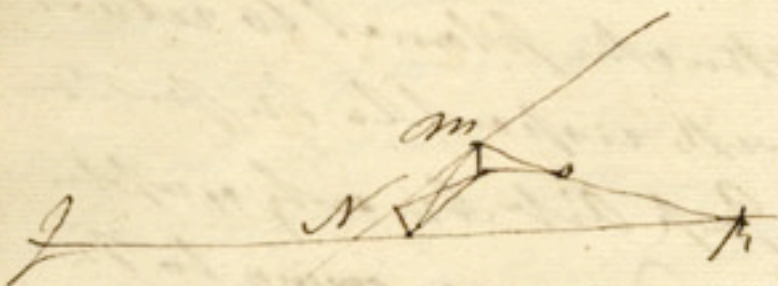
not. The axis another orbits  
i.e. a revolution of the nodes



Effect of an planet  
on the orbit of another planet  
is to make the nodes of the  
other planet to retreat  
with respect to the perihelion  
J<sup>r</sup> orbit. The only exception  
is advances. owing to the  
action of Saturn

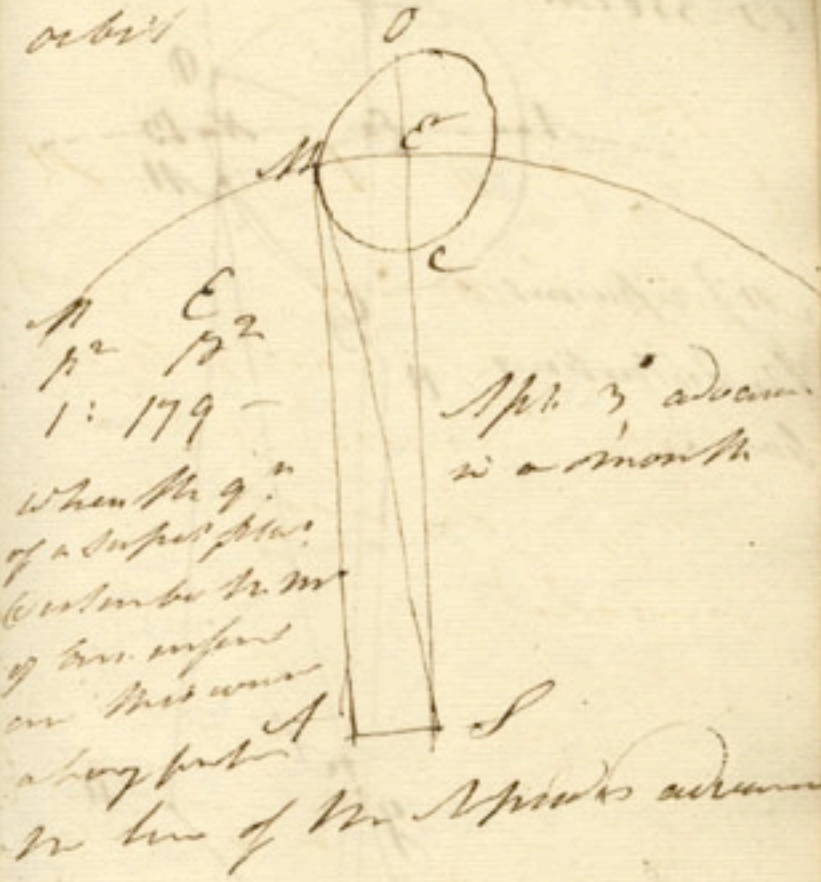


Int. of the orbit constantly  
 altered when approaching to M.  
 and it is increased when  
 receding from the node it is  
 diminished.



True inclination constantly  
 between each other also the  
 mean M<sup>d</sup> between each other  
 at the end of every revolution.

Orbit of the Moon  
 orbit



M E  
 179 -

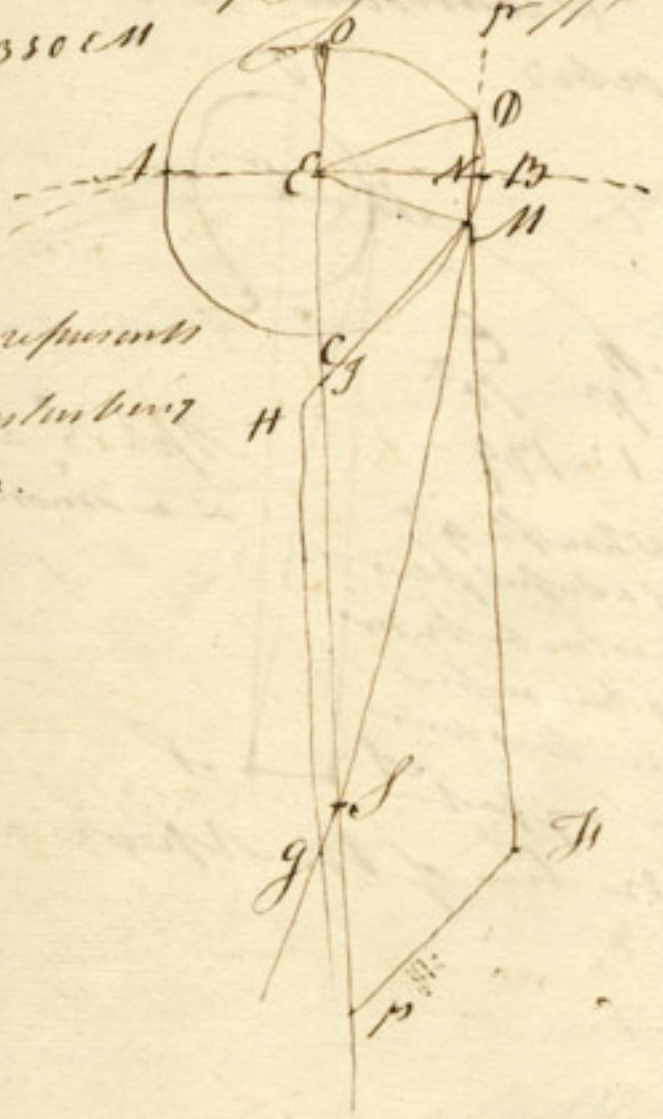
When the 9<sup>th</sup>  
 of a Superfluous  
 Orbit to the M<sup>d</sup>  
 of the inferior  
 on this was  
 along with  
 the line of the Moon's advance

Apr. 3<sup>rd</sup> advance  
 in a month



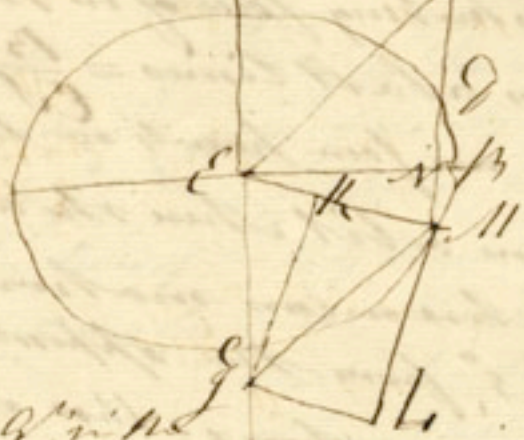
CG = 330 CM

15 Jan 1776



II] represents  
the disturbing  
force.

16



Moment of the  
conjunction dimi-  
nished as much as in the quad.  
augmentation of the quadrat  
is  $\frac{1}{179}$  part of the whole  
gravity - at the conjunction  
it will be double this quant  
 $= \frac{1}{90}$  nearly.

A

The true force of the  
 Moon at all times =  $\frac{PE}{ES}$   
 There are four points in the  
 Moon's orbit where she will  
 have her mean motion -  
 viz 45° from the opposition  
 and conjunctions. This is  
 not quite accurate, tho' affirm'd  
 by some Philosophers.

The Moon's place is the  
 same at the Syz. and Equinox  
 as if she had moved equally  
 The Moon nears the Earth  
 at the Equinox than at the Syz.  
 The Moon's orbit on the Earth  
 is well known very little error  
 Out from the Syz. 44°  
 54° 35'

16 Jan<sup>y</sup> 1776

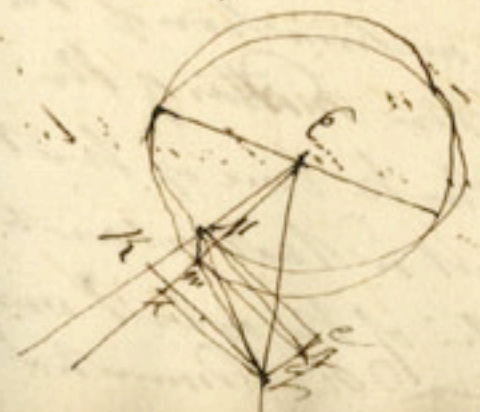
Equi. of the  
 orbit is about  
 from 5 to 7½



The diameter  
 of gravity in the  
 Apodes which  
 they consider to be  
 Syz. They advance  
 but when they have  
 of the Apodes is  
 in the Equinox they  
 repeat.

- The position of  
 the orbit is also  
 altered

Upon the whole  
 the Lunar Apodes  
 advance about 3' every revolution.  
 - The Moon's orbit is inclined  
 to the plane of the Earth's Equator



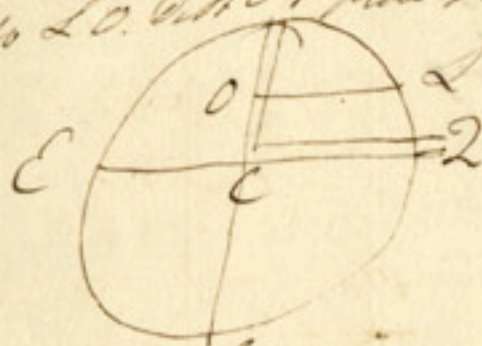
The moon when leaving the  
node west by the action of the  
Sun's gravitation is an orbit left  
incl. to the Ecliptic by which  
the node is removed to the westward  
- When the moon approaches  
a node the inclination of the  
orbit is increased & the node is  
still moved backward.

When the Moon is in the Sol.  
the Sun is in Nodes  
Nodes in the quadratures  
In these three cases the action  
of the Sun will produce no alter-  
ation in the inclination of the  
orbit or in the position of the  
nodes - When the time of the  
Sun is the first or last octant  
the inclination of the orbit will  
be more or less disturbed

Nodes in the 9. Moon in the  
Sol. produce the greatest in-  
crease of inclination on all points  
and supposing the force of  
the Sun the same - In winter  
the time of the Sun is about 24'  
greater than in summer  
hence owing

17<sup>th</sup> Jan<sup>y</sup> 1776

Of the figure of the Earth  
was the earth flatter at the  
poles & be a spheroid. But the  
curvature at four will not be  
any part of the Earth  
from the center just a few  
to L. O. Dist<sup>n</sup> from the center

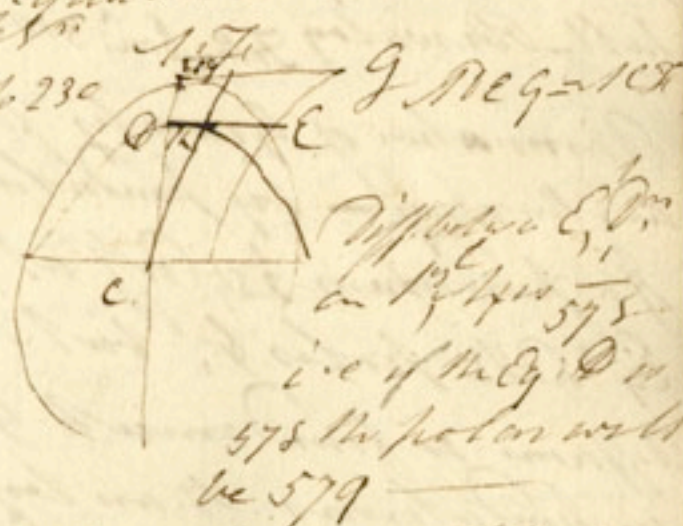


Several from the north to the center  
at the center to the 2  
whereby rings show the figure  
of the earth, but not justly  
because there is an auric  
form which is not in the earth

The same thing will happen  
tho' the earth be partly spheroid  
& partly round. — In the Moon  
as or high at the Equator as  
at the P. we may consider the  
Earth. has yielded to this form  
To determine the figure of the  
Earth  $\frac{2}{4}$  such a part center C, F.

$\frac{1}{259}$  of the gravity of the spheroid  
on the Equator = Cen. F.

In F. 1<sup>st</sup> 229 to 230



Difference E, P  
on 1<sup>st</sup> 1/2 578

i.e. of the Earth is  
578 the polar will  
be 579

this will be the case if the Earth  
is a homogeneous body

Gravity of any part of it will  
 tend to the center but a little  
 towards the Equator. It is also  
 altered by the super-incumbent  
 matter at the Equator on both of  
 these accounts the earth which  
 it would be from the C.F.  
 True figure can only be had by  
 measurement alone - there have  
 not been made with sufficient accuracy  
 Summit changed -  $304:305$   
 $210:211$   
 Hill - Observatory John Doni  $310:311$

Determination of Gravity found  
 another way - by pendulums  
 of a pendulum  $289$  Diff at the  
 Equator the poles &c. but the  
 difference is found much greater  
 in pendulums than by the  
 measurements, by w. the C

In Just: The axis of Earth  
 or by N. Prob: 12: 14 -

In the Sun  $37000$  part Diff -  
 a quarter by too small for observ.

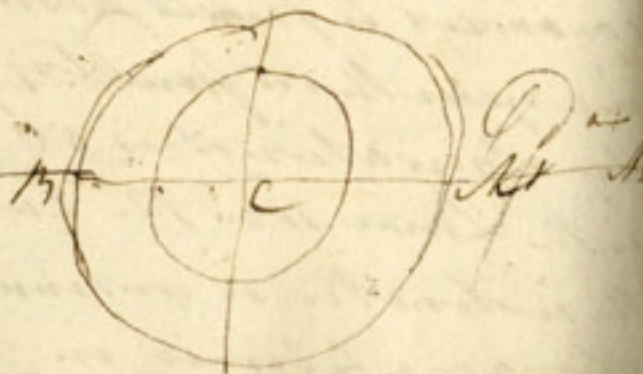
A ring of moons adhering to earth  
 it will wind up all the change  
 that take place in the moon  
 (immense) till it touches the  
 earth the consequence &c - Mett:

at the Equator constitutes such  
 a ring. The joint action of the S  
 and M on this ring makes the  
 equinoxes to precess about  $52''$   
 in a year this is found by calcul  
 - by observation it is  $50''$ . As  
 in the Lunar so in the Earth  
 the inclination is continually  
 changing 4 lines in the  
 year sometimes slower faster

The poles of the Earth wret  
in 25920 years this round by

of the Tides

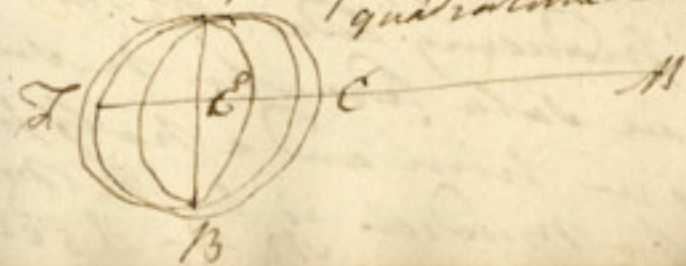
Earth and moon tend to  
each other - Every particle  
on the surface of the Earth will  
have its  $\frac{1}{2}$  of its mass by its  
tendency to the moon - this  
will be in proportion to the  
accumulation on the waters  
Elevation on both sides



This - inequality of the Sun's  
action on different parts of the  
earth, and the difference of the  
centrifugal force arising from  
rotation of the Earth and moon  
round <sup>their</sup> common center of Gravity.  
The action under the moon is  
than the opposite.

18 Jan<sup>r</sup> 1776

This is a true cause of the  
Tides. The greater a Mass  
of the Earth  $\frac{1}{2}$  on the particles  
at Earth  
will the  
water of  
the Earth -  
The obliquity  
of the Moon's  
Orbit.

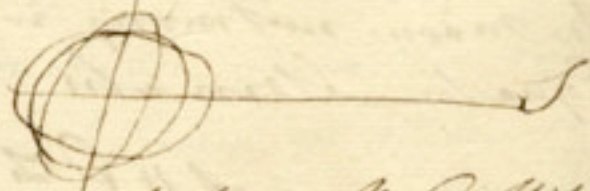


By the revolution of the Earth from West to East every place would have two tides in a ~~day~~ day - Moon moves to the east - High water not when the moon is on the Meridian. If the water met with no resistance high W would happen 3 hours after the moon passes the Mer. but the friction of the water the tide is about  $1\frac{1}{2}$  hours <sup>or 2</sup> from <sup>the Mer</sup> W. <sup>the Mer</sup> of tide under the moon -

3721: 2600 3  
 05. 08-  
 119: 121

Sun also operates on the earth in producing tides. We should have solar tides when the sun is on the Meridian and a half past the Meridian is by the Moon  $\frac{1}{50}$  S 5625

At the time of new and full the tides ought to be greater but w<sup>th</sup> the Moon in the quadratures. The actions of the Sun and moon oppose each other N



hence it follows the difference between the Ebb and flood is greatest at the spring tides and least at the neap tides. Tho' the action of the Sun is greater than that of the Moon on the earth yet it does follow the Moon because the diff<sup>erence</sup> of the actions on the surface; center, and of volume of the earth is much greater than

Part of the sun on account of  
his great distance from the earth.  
At Newbury forces are in  
the moon:  $\therefore$  therefore the  
tides greater in winter than in  
summer.

of Atlantic is less from  
the moon: not more in the  
Equator - It is also

at 14  $\frac{1}{2}$  hours  
can be lost outside  
a day - M



when the moon is on the same  
side of the equator with the spot  
the day side is the greatest and vice  
when the moon is under the meridian  
in the Equinoxes the tides ought  
to be nearly equal

That the tides may have  
the full effect it is necessary  
that the sea should extend at  
least to  $90^\circ$ . Hence we can expect  
no tides in the West: Baltic:  
A greater tide at the north  
and south of the Atlantic, than  
in the middle. Great tide in  
the English Chan: on account of  
its situation - Tide up more  
happens rather. Few in the  
German ocean - At Dover very  
irregular on account of Strait  
situation between two seas:  
M S  
1: 25000000 } 1: 289 | 2  $\frac{1}{2}$ : 1  
1: 13,000000 }  
1: 44000 } Effect of the sun to  
E & S 90000 } raise the water about  
and by them } 2 feet



Now an argument in  
support of the Copernican Syst.  
From the different actions  
of the sun and moon on the  
Tides we calculate <sup>the</sup> quantity  
of matter in each  $\&c.$  by pro-  
ceeding in this manner we find  
the center of gravity between the  
sun and earth is <sup>the</sup> in the body  
of the sun, and the center of G<sup>ty</sup>  
between the Earth and Moon is  
the point where they sit near  
it, and which observation con-  
firms.

18<sup>th</sup> Jan<sup>y</sup> 1776

Of the Aerial Tides —  
The change in the Atmosphere  
would be  $\frac{1}{50}$  inch which would  
be be observable on the Barom:  
if the Atmosphere was = Semi D:  
Earth. — But the Earth's Atm:  
not so high — and much rarer —  
— Trade winds owing in a great  
measure to the aerial Tides —  
— Supp: the Moon covered w<sup>th</sup>  
water Tides in the moon = 94  
Suppose this mass should freeze  
or turn solid and projected  
round the earth. The action  
of the earth on this egg like figure  
by accumulation will at length  
bring one side always to face  
the earth. This motion not

10. A B M. un. M. Th. ad  
 of any given line will move  
 M. un. the space in the  
 H. ~~structure~~

10. Any body falling from a given  
 space acquires a velocity which in the  
 course of M. un. time that space is the  
 same time

$$32.2 = g \quad \left\{ \begin{array}{l} h = \text{height} \\ t = \text{time} \\ v = \text{velocity} \end{array} \right.$$

$$h = \frac{t \times 32.2}{2} \quad \left\{ \begin{array}{l} \text{any time formula} \\ \text{with a given } h \\ \text{or } t \end{array} \right.$$

$$v = t \times 32.2$$

$$t = \frac{\sqrt{2h}}{5.674} = \text{sq. root of } 32.2$$

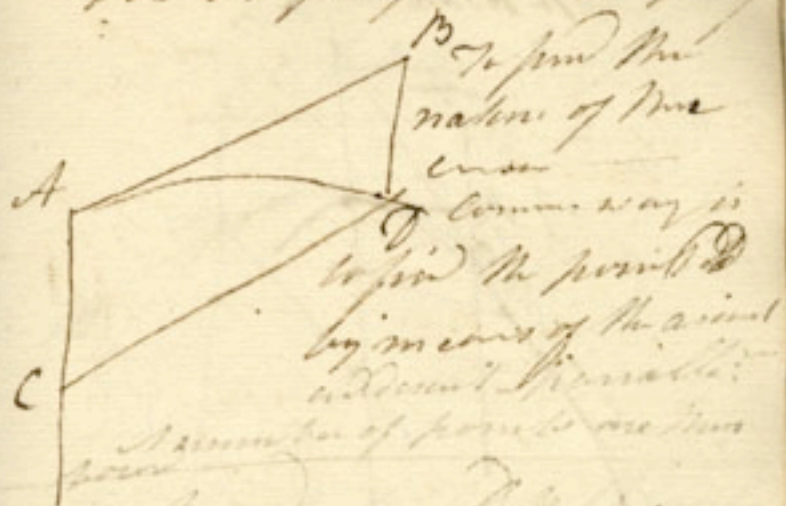
$$t = \frac{v}{32.2} \quad \text{using } v \text{ as any body} \\ \text{with a given } v$$

$$h = \frac{v^2}{64.4} = \text{to which } h$$

a body will rise

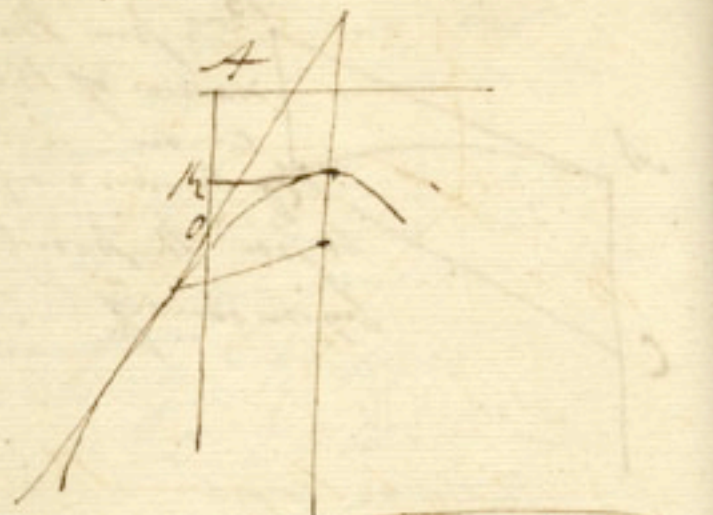
These two formulae  
 respect bodies let  
 fall from any height

Bodies projected obliquely

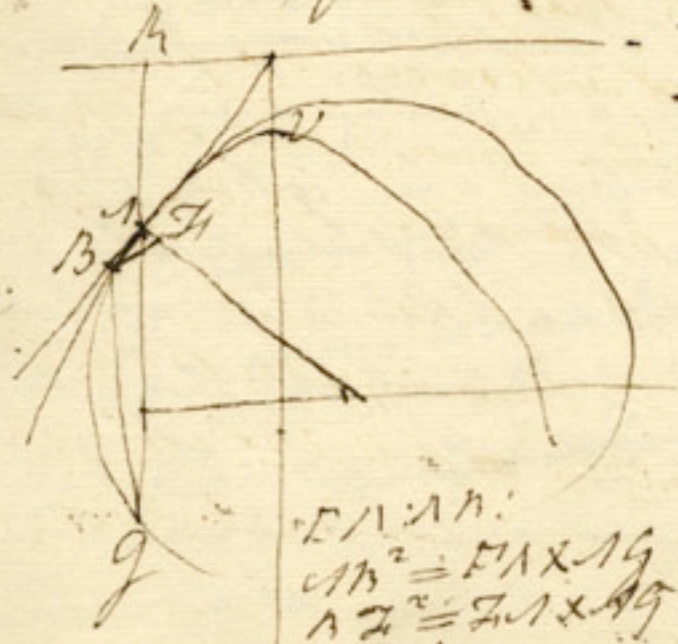


to find the  
 nature of the  
 mass  
 of common way is  
 to find the provided  
 by in course of the aerial  
 without difficulty.  
 A number of points are thus  
 given  
 A 25. p. would find a  
 bullet 5 miles perpendicular  
 if it met with no resistance from  
 the air, but on account of this  
 resistance it's height & range  
 will not be it above  $\frac{1}{2}$  of this  
 height a little more; therefore  
 the gravity of any body at still  
 the different distance from the  
 center earth, which we cannot  
 easily experimentally see may with  
 any sensible error be supposed to be

Point



22 Jan 1776



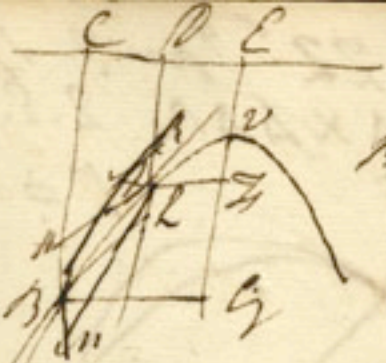
$EA:AN:$   
 $CB^2 = EA \times AG$   
 $AZ^2 = ZA \times AG$

22<sup>nd</sup> Jan 1776

$BZ = ZA \times AR$  2.E.D.  
 $r = \frac{v^2}{ch}$



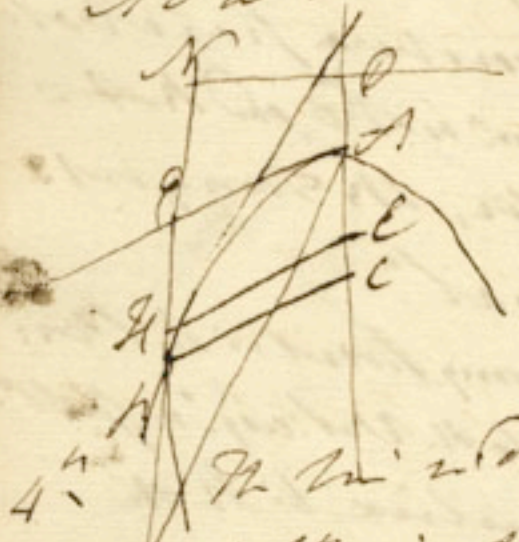
If a body falls from A to B  
 and then projected along AB  
 it will describe a parabola  
 whose diam. is AD, and AC =  
 $\frac{1}{2}$  parameter, AB tangent.  
 " Coroll.  
 Vel. at any point in the Par.  
 will be = to H. Vel. acq. in fall  
 from the incline to H of  
 point.



$$AC:AD:V^2:v^2$$

11.  $V$  at  $A$  to  $V, B$  with  $H$   
 in  $BA$

111. Terms of describing the arcs  
 $AV$  and  $VB$  ::  $DE$  and  $EE$



4<sup>th</sup> The  $AV$  is described by  
 any  $AV$  is =  $t$  to  $AV$   
 the  $AC$

$$t^2 AB : t^2 GC = \frac{t^2 GC^2}{v^2 AB \cdot v^2 C}$$

$$t^2 AB : t^2 GC = \frac{11B^2 - HC^2}{13B^2 : CD}$$

$$11B^2 : 78C : 13B^2 : AV$$

5<sup>th</sup>  $t^2 AV \cdot AB = t^2 AV \cdot AC$   
 with an uniform motion at  
 $A$ .

The principle of the great  
 in cannon - present blanks  
 at low yards distance every  
 with cannon being thicker  
 at the breach than at the  
 muzzle - if some were in truth  
 shot along the Dutch by Mr.  
 Vanborn - Chief use of  
 the 3 for some shells.

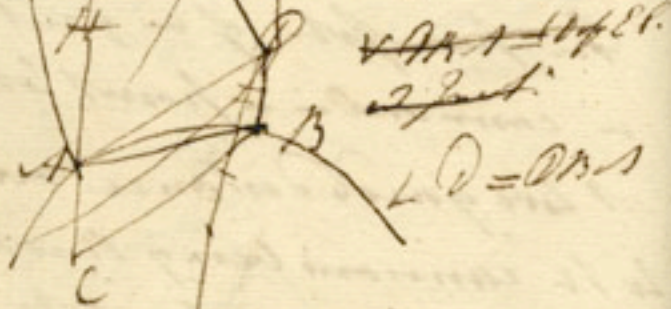
Weight of Shells

1 q<sup>m</sup> L<sup>2</sup> & D<sup>2</sup> = Line of Direction

11 q<sup>m</sup> . D<sup>m</sup> D<sup>m</sup> = Force or g<sup>1</sup>

111 q<sup>m</sup> g<sup>m</sup> g<sup>m</sup> = Time

Case of Design the Force or imp<sup>1</sup>  
and the Distance to find the Line  
of Direction or angle of Inclination?



$AD \times AD = AD^2$

$AD \cdot AD = AD \cdot AD$

M<sup>r</sup> Vanbrue first introduced  
the method of throwing cannon  
balls parallel to the Horizon  
with small quantities of powder,  
chiefly designed to kill men  
along the trench. - Refugees being  
left upon the out works in two  
troops them about 4 or 500 yards  
distance. They approach near  
as we - till they arrive at the  
trench about 80 yards from the  
port. - As the besieged are com-  
monly secure from horizontal  
shot it is necessary to be able  
to hit them in another direction.  
Hence the invention of bombs, wt<sup>1</sup>  
are thrown so as to fall nearly  
perpendicular to the roofs of  
houses powder magazines &c.

The whole business of Gunnery  
may be reduced to three parts.

- I. Having given the Force and  
Distance to find the true of  
Direction, or angle of incline;
- II. Given the Direction and Dist.  
to find the force & range
- III. Given the Horizontal Dist.  
or Direction to find the Imp.

23 Jan<sup>r</sup> 1776

Great range when the angle  
of Elev. is 45°. It must be  
known within what time by means  
of a Gunner and a plummet. When  
the object is placed on a horizontal  
plane the angle of Elev. must be 45°.  
Horizontal ranges at Diff. are ::  
sines

It is difficult to trace the path  
of a single body because it leaves  
no trace - but this can be  
done by the continuance -

Exp: Fountain - Curve more  
concave near the place of fall. This  
very remarkable in a shell -  
Line of the rise of a shell to its  
fall, at best is as 5 to 3

range about 45 should mean  
the corresponding range below  
the horizontal range more the  
less the impetus by experiment -

19<sup>o</sup> 445  
10 330 should be 620  
8 690  
4 600 = 330 to 27

To find the impetus  
by receipt of the shell  
To find  
ball 24 inch diam 45  
with the weight of 37  
the powder 16 45  
the 16 inches 400  
10 430 700  
1400 (the 1/2 in)  
1690

Cause of the difference between  
the Theory and experiment -  
1. Resistance of the air - greater  
in greater velocities in proportion  
than in smaller - i.e. each square  
of the velocity will 1000 feet of air  
between some 1100 feet the resistance  
increase very fast it is doubtless

11. Curvature of the projected body  
occurs before resistance  
has water involved more than  
distance from shot mass than  
width of it.

Exp. Bull. at a height  
ent. 25: 1670 } velocity  $\frac{1}{2}$  second  
75: 1527 } 127 as a Maxim  
125: 1429 } Let  
+ its weight  
ent or  $\frac{1}{2}$  inch width  $\frac{1}{2}$  = 10  
at height of fire

111. Difficulty of directing the  
fire - windage - when  
it comes to fire it may not  
go in a straight line. This  
remedied in most as by wedges

The projection of a jet of water  
may be easily measured it  
is equal the perpendicular height  
which should by the Theory be  
=  $\frac{1}{2}$  Height range at  $45^\circ$  by Exp.  
however it turns out little <sup>less</sup>  
than the whole range.

By Mr. Theory the time of rise  
should be equal to the time of  
fall, in small projections this  
is nearly the case, but in practice  
it is very different Exp. M.

The time of the rise of a shell  
from the distance of  
to its fall was nearly as to

By Mr. Theory the Horizontal  
range above  $45^\circ$  of fire should be  
equal to the correspondent range  
below, but they are found by  
experiment to be much shorter.



The impetus of a piece of Ordnance cannot be so easily measured as that of a Jet.

It may however be determined pretty nearly by the recoil.

The recoil of a piece will be  $m::$  to the force impressed on the bullet, as the weight of the bullet to the weight of the piece. By knowing the recoil in small quantities may be found by experiment and thus we can find know deliberately of our properties.

Since the results of experiments are so different from those of the theory, the theory is of little use to direct the practical Gunner.

The cause of this deviation one is 1. The resistance of the air this increases as the square of the velo: nearly, consequently

the greater the ranges, the  $q^2$  will be the deviation, In experiments made in a room the deviation is small, but very great in shells.

The deviation will also be much greater in light than in heavy bodies, because the resistance of the air ~~is~~ bears a greater  $q^2$  to the force than the latter. Hence the deviation of water is more than an iron bullet. &c.

11. Another cause cause of deviation is the difficulty of directing the piece to the object, or to any angle of elevation, this arises from the shape of the cannon or mortar & its shock at the breach than at the muzzle. Besides the wind may occasion a considerable deviation. This last cause may be partly remedied by putting

into the mortar pieces of wood  
in the form of wedges very thin  
at the upper end between which the  
shell is kept in the middle of the  
charge. —

The Impetus may also be  
found tolerably exact by making  
a bullet strike some obstacle  
that may be carried along with it  
such as a pair of lead. By this  
means the impetus may be de-  
termined within  $\frac{1}{20}$  of the truth.

In this manner Mr. Robins tried  
the following experiments —

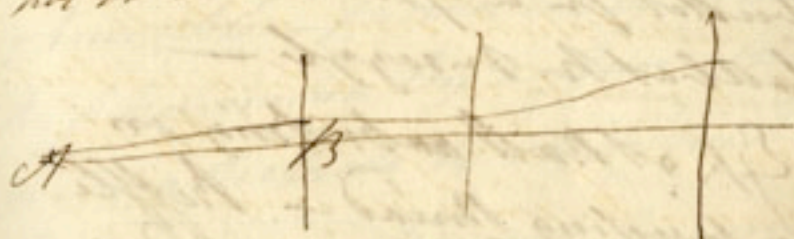
A bullet  $\frac{1}{2}$  lb weight was thrown  
250 paces its velocity & second 1676,

Again it was thrown 75, its vel<sup>ty</sup>  
was then found to be 1527. It

was again thrown to the distance  
of 125 its velocity was then found

the <sup>with weight</sup> resistance was found to be as 121:1  
that is the resistance at leaving the

piece was about ten pounds  
Whether in the flight of a projectile  
it should still move in the plane  
of that figure. In this respect there  
was great dissension and some  
flight neither in a horizontal  
nor in a vertical plane —



Mr. Robins observed that a  
bullet has not only a  $M^o$   
of progression but also a  $M^o$   
of rotation. This is evident in  
bodies thrown by the hand  
also in shells as seen by  
the flame in the night  
The last stroke which the  
bullet receives on leaving the  
muzzle determines the axis of

24 Jan. 1776

rotation. Expt. by N. Wilson  
The few bullets Miss paper  
screens from a Gun fired from by  
to a block of wood - Miss  
was composed by firing a  
bullet in a Gun burst a  
bullet in the muzzle -

Expt. A Ball embarking on  
a twisting thread - Ruffle  
Gun. Sawed chare reminds  
Miss direction

What is the cause of Gravity  
Quartes Vertues - Phil. Phil.  
attribute of the action of  
a fluid - Action of Gravity  
as particular as percussions &  
the two sets of facts are equally  
observable - In order to explain  
the phenomena by a fluid we  
must attribute to this fluid  
properties unknown to every  
other fluid.

Of Mr. commencing  
by the public

Series of bodies in: not to the  
squares of their velocity. Mr.  
Poisson was attempted to be done  
by Leibnitz by three sorts of  
experiments. I. Bodies thrown  
upwards. II. Bodies striking  
against soft bodies. III.  
Bodies bending springs.

When two bodies have the same  
weight & the same velocity the  
forces will be equal. - Ex.  
two equal pendulums of soft  
clay let fall from the same  
height will destroy each other  
motion, if the directions are  
opposite. - The direction of the

by opposite motion is a proper  
test of the equality of forces  
Ex. - A ball of clay let fall  
in 4 water half to gain.  
In 2 in opposite direction  
destroy each others motion  
then the V. are inversely as the  
quantity of matter.  
Hence the forces are: velocities

To examine Leibnitz Ex.  
it is true that a body projected  
with 4 times the force will  
run to 2 Distance - Three  
kind of obstacles objects that  
are immovable with regard to the  
striking body. II. A resistance which  
the body can just overcome and no  
more. III. A resistance from an obstacle  
which a striking body can carry along  
with it.

25 Jan. 1796

Newton's Method: Graves: Leibniz  
mean the forces are :: to be  $V^2$  the  
end of  $V^2$  action -

1<sup>st</sup>ly; 2<sup>nd</sup>ly they are speaking of the  
moving power when the  $v$  is velocity  
speaking of the effects! All force  
is depend on dispute in van, this  
cannot be done abstracted from  
quantity. Only an ampliation

of force a good definition i.e. the  $V^2$  is  
is a proper measure of force. If

the  $V$  mean by the  $v$  is  
a definition this can be no error  
but to say that  $v$  is not this

may attempt to prove that the  
forces ::  $V^2$  they take for granted

that the heights are the measures  
of the forces, this is not the whole  
effect, the time must also be taken  
into account.

Study projects 32 feet in a second  
will walk from him the force was  
less but then it takes 2 seconds  
therefore the forces are ::  $V^2$   
By the Hgh: of the Gun: it is im-  
possible to account for the violence  
of hard bodies

A body striking a soft body with  
double the vel: makes 4 times the im-  
pression - this does not prove the  $V^2$   
because each parcel of the soft body  
acts but for one half of the time.

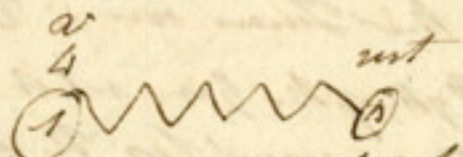
We have sometimes a measure of  
force independent of the effects

Thermometer does not measure  
the quantity of heat in the fire

but its effect in the expansion be-  
cause can meas: the quantity

of heat independent of the effects -  
a pint of warm wet: a pint of Oil:  
will hold double the heat -

A more elastic bow 2. It goes on  
with 2. - But when El; Above  
it's whole motion. But of both



El: It will move backwards  
Zur: Effect is that the same  
with interchanged V's

If the impulse is made obliquely  
the whole force is not employed  
in producing the stroke



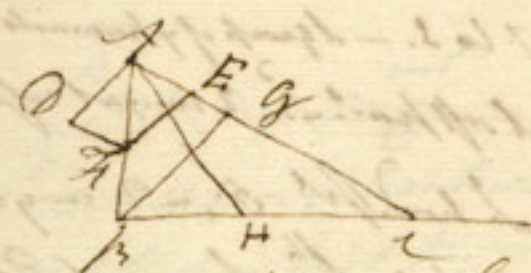
Eff: It is similar to the  
to compare a direct  
with an oblique  
stroke. multiply

The vel: into the sines of the resti-  
tion angles i.e. radius and the  
angle of incidence - Useful -  
a ship sails, from

26 Jan 1776

July will abound with a vel:  
∴ to 7 to 8. - A group of 4 points -  
1. 2 equal soft part. - 3. 2 unequal soft part  
4. 1 equal hard part. 5. 1 - 2 unequal  
6. 1 equal part. 7. 1 equal El: part  
- application to the hand when the  
water is thick. When the V's are  
small not above 70 F. of the  
it will ∴ as only as V<sup>2</sup>

Quat. applied by construction  
 - products -



AC: AD: AB: AC: Long plane  
 This for along the plane is  
 constant. Hence all the qua-  
 ties of perpendiculars in descent  
 are applied here AB and G:  
 AC: AD. - times of descending  
 as the length of the plane  
 to the height, cont.

Time the motion along an inclined  
 plane is uniformly accelerated  
 as always time to distance

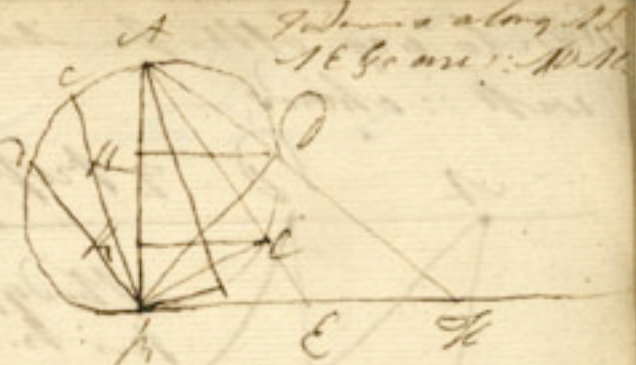
$$\begin{array}{r}
 1 \text{ h:} \quad III : V \quad 0 \\
 K : \quad IV : VI : 0 \text{ ch} \\
 \hline
 h : 3 : V : 0 \\
 K : IV : 6 : 0 \text{ Prod.} \\
 \hline
 \end{array}$$

1A

O V III A  
 O W VI K  
 O V C A  
 O U VI K

A

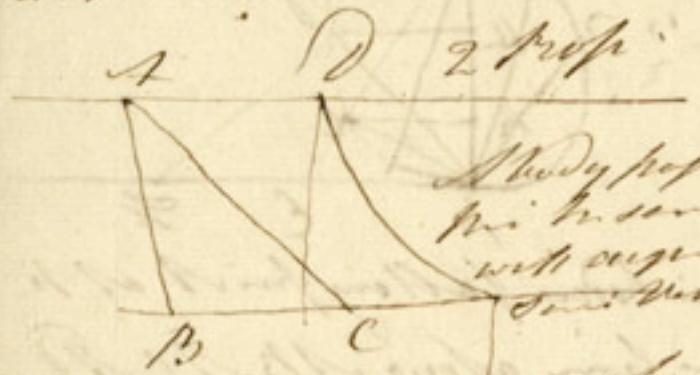
Cor 4  
 2  
 2



The bodies falling first at the  
 same time along AB, AC, AD  
 they will arrive at the points  
 B, C, D at the same instant  
 The velocity at the point C  
 will be as the length of the chord  
 along which they descend. The  
 wooden circle divided into chords  
 The force of the air on a  
 chord. of descent. Robert  
 Descartes along the air resistance  
 along any chord.

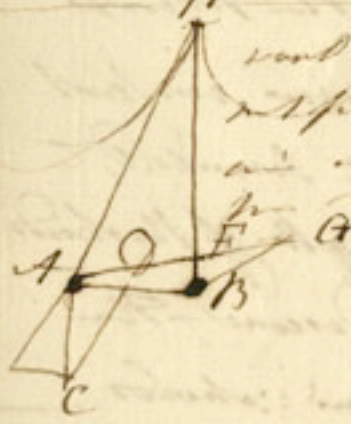


<sup>en</sup>  
 The velocity of all points D: C  
 will be chords



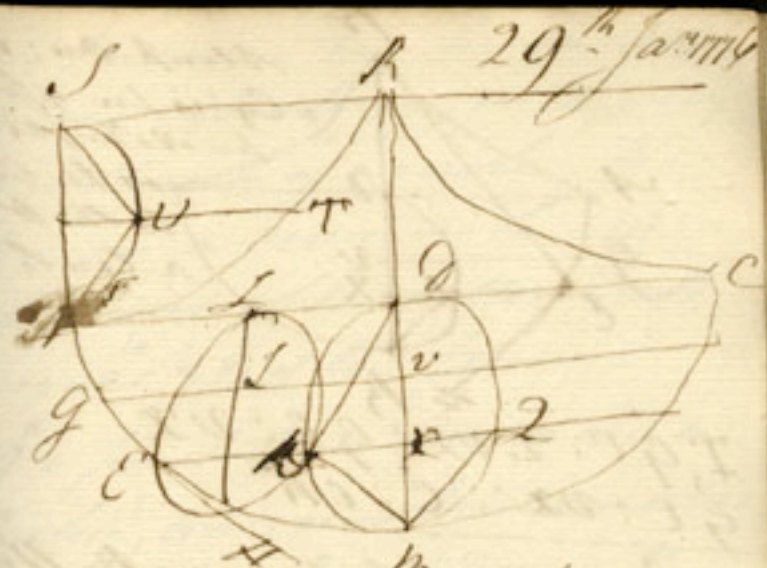
A study prop:  
 The to see the  
 with angles to  
 some what.

The curves must be constructed

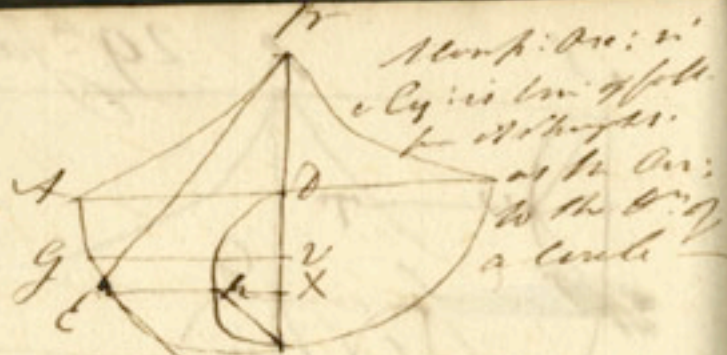


would move out of the  
 and to the center of the  
 and the force that  
 the part of the force

Saturday - 27<sup>th</sup> Jan<sup>ry</sup> 1776  
 A Lecture upon Comets



$SC =$  circumference of circle  
 $SG =$  chord  
 $EH =$  chord  
 $EB = 2 \text{ chords } EB \text{ Gen. Circle}$   
 $EM = 2 \text{ chords}$   
 $GE : vx : PM : RZ$   
 $GA B$  to show  $AB$  and  $BC$  in the



$T, G, E :: T, V, X :: G, E :: V, X$   
 $G, E :: V, X :: C :: Ch$

Times in diff. Cyc: are as the  
 heights of the Cycloids or the  
 times as  $\sqrt{\text{Height}}$  squared

Times of any vibrations in a  
 Cycloid are all equal

$$T^2 = \frac{S}{F} = \frac{S}{J}$$

If the vibration of a circular  
 pendulum be in a small  
 arc it is equal nearly

$29:34$

As  $16000$   
 to  $16001 \frac{2}{3}$

If there are two pendulums  
 the one vibrating in a very  
 small arch of a circle, the  
 other in a semicircle 29  
 vibrations of the latter will  
 be equal  $\frac{3}{4}$  of the former

If a pendulum moves in a  
 Cycloid, and another describes  
 an arch of  $1^\circ$  of the  
 vib: of the latter will be =  
 $\frac{1}{2} \sqrt{201 \frac{2}{3}}$  of the former

Time of a  $\sqrt{V}$  will be nearly  
 as the circumference of a circle to  
 its dia.

Very small V. are in the sub  
 spherick part of the length  
 i.e. a pendulum to vibrate  
 twice as slow must be  $\frac{2}{3}$  times  
 the length

31. Jan. 1776

Effi. pond. with ~~curve~~ curve  
to see height whatever is the  
nature of the curve of Descript<sup>n</sup>  
Application

The pendulum is made to de-  
scribe two different curves, by  
interposing an object between  
the string, it will not be the same  
ing in both same height on  
both sides.

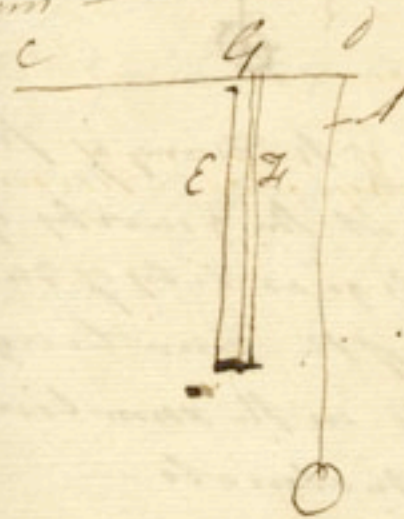
The Glass - w<sup>th</sup> glass - Case  
<sup>of the</sup> of the a curve. w<sup>th</sup> G - Lion  
Dials by Anaximander - Not  
brought for - Syr. to Rome  
Invented for the equation of  
About the 7<sup>th</sup> & 8<sup>th</sup> Century water clock  
a curious one by Dribben, where  
the vessel was so shaped that the  
water run out equally - Some  
was made with a wheel turned by  
a spout of water. First clocks were  
regulated by a fly like a Jack -  
In suspensions - After wards it was

improved by changing my the pro-  
 gressive anchor into a respro-  
 cating M<sup>o</sup> - Balance - Dr.  
 Hook greatly improved Miss M.  
 by adding a spring to the rear  
 of R. Bell - Watch - The quaker  
 watches move so much the better  
 they are - common ones about 6  
 beats in a second - Harrison's  
 watch - This improvement  
 cannot be introduced into a com-  
 mon watch on account of its size

N.B. This day Sat! Thermometer  
 at 14<sup>o</sup> -

1. Feb. 4 1776

Estm moved the anchor on the  
 quant. of M<sup>o</sup> in the fluid, in order  
 to increase the momentum. The first  
 method seems the best - can move  
 A Clock kept time within a second  
 P. Brown - That of hands the rod -  
 M. Graham's M<sup>o</sup> pend: rod -  
 M. Harrison's compound pen-  
 dulum -



Harrison's pendulum



Another use of the Theory of pend.  
 is to prove that the quantity of any  
 body is :: to its quantity of matter.  
 pendulums of the same length  
 will vibrate in the same time  
 whether the weights —

How we can very accurately  
 determine the time of the descent  
 of heavy bodies — which cannot

be done accurately any other way.

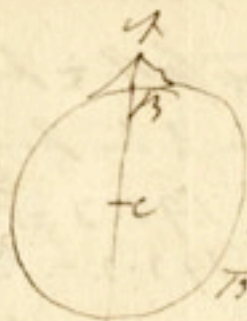
22:7: TV  $\frac{1}{2}$  time fall.  $\frac{1}{2}$  pendulum  
 22:7 1:315 time  $\frac{1}{2}$  the pendulum  
 $+^2:315^2:19.6:193.3 = 16.11$   
 315:1 19.6:193.3 = 16.11

This gives us a very accurate measure  
 of the accelerating power of gravity

If we find <sup>the time</sup> the pendulum makes a  
 given n<sup>o</sup>. of vibrations in a day we  
 may conclude the power of Gravity  
 at that place

95770 } in a day near the  
 95740 }  
95720 }  $439.7$

M. Bouguer {  $438.9$  ~~2474~~  
 $438.9 = 2474$  falls  
 upon the  
 level of the



$$1348 = BC$$

$$1349 = AC$$

that is the height is  
 $\frac{1}{1348}$  of AC

$$1348 : 1349 :: 439.7 : 439.1$$

$$1348^2 : 1349^2 :: 439.9 : 440.3$$

Since the gravity as we ascend from  
 the surface does not diminish so  
 fast as the  $O^2$  - Here the Reflection  
 of the planet was not taken into  
 account.

These experiments will also show  
 in what  $\therefore$  the gravity increases  
 in  $O^2$ : Let this be taken into  
 the account: 'then that gravities  
 are not  $\therefore$  centrifugal force  
 situation of observatories must  
 be enquired into

In order to increase the accuracy  
 of a pendulum we must either make  
 the pendulum very heavy or make it  
 vibrate in large arches: This last  
 seems to be the best method, because  
 when the pendulum is very heavy  
 it communicates a motion to the case  
 or support of the clock which alters  
 the vibrations of the pendulum —

By the pendulum we obtain  
 a very accurate measure of the  
 time of falling bodies. For the  
 space of a second is so short that  
 we could not observe within  $\frac{1}{3}$  or  $\frac{1}{2}$   
 of the truth. but by knowing the  
 $\therefore$  of the times of Vib. to the length of  
 bodies &c. we can find the time of  
 descent in a second. — By making  
 the pendulum & perform 8400  
 Vib. in a day we get one Vib. in  
 a second very accurate.

2. Feb. 1776

Motion of pendulums not in  
 fact at all in a point - Centre of  
 Oscillation in a prism not  
 in the centre of the prism but  
 but  $\frac{2}{3}$  from the point of suspen-  
 sion

Expt. A prism and a ball  
 $\frac{2}{3}$  of the former are Isochronous -

Two equal balls one at the  
 middle and the other at the  
 lower end of a prism, will be  
 Isoch. with a pendulum  $\frac{5}{6}$  of  
 the former, and not  $\frac{3}{4}$ .



$$\begin{aligned}
 1 \cdot 1 &= 1 \times 1 \\
 1 \cdot 2 &= 1 \times \frac{1}{2} = \frac{1}{2} \\
 \hline
 1 \times 1 + 1 \times 2 &= 5 \\
 1 \times 1 + 1 \times 2 &= 7 \\
 \hline
 1 \cdot 2 &= \frac{5}{3} = \frac{5 \frac{1}{3}}{6} =
 \end{aligned}$$

N.B. This is true in a straw -



2. *Calculation*

$$P.A. = 2 \quad 2 \times 4 + 1 \times 9 = 17$$

$$P.B. = 3 \quad 2 \times 2 + 1 \times 3 = 7$$

$$P.O. = \frac{17}{7} = \frac{17}{7} P.B.$$

103  $P.O. = \frac{17}{7} = \frac{17}{7} P.B.$

102  $P.O. = \frac{17}{7} = \frac{17}{7} P.B.$

Exp. 31 A *Calc.*

$$P.A. = 1 \quad 1 \times 1 + 1 \times 4 = 5$$

$$P.B. = 2 \quad 1 \times 2 + 1 \times 1 = 3$$

$$P.O. = \frac{5}{3} = \frac{5}{3} P.B.$$

The Centre of Gravity is found  
 P.O. by a parallelogram whose  
 area is the product of  
 each part of the matter into  
 the square of its distance from  
 the point of suspension and the  
 Centre

Effect of any pocket

$$x^2 \times x \text{ fluid is } \frac{1}{2} x^3$$

$$x \times x \quad \frac{\frac{1}{2} x^3}{x^2} = \frac{\frac{1}{2} x}{1} = \frac{1}{2} x$$

Therefore  $P.O. = \frac{2}{3} H$

In this calculation the thickness  
 of the rod is not taken in to account  
 then we will make some alteration  
 in the Prob.<sup>n</sup>

Exp. 32 A triangle with a great base  
 its vertex the centre of Gravity  
 will be  $\frac{2}{3}$  from the point of Support  
 this is more accurate when the  
 triangle moves edge wise.

Exp. 33 Triangle with a great base  
 moving edge wise slow. Math  
 otherwise -

Eq. of pyramid  $\frac{1}{5}$  about its  
vertex the Cent. of Earth at  
 $\frac{1}{5}$  whole length

To find the Center of Os: of a second  
perpendicular

$2r$  = radius of the ball

$d$  = dist<sup>ns</sup> from Center of Earth to  
the ball to the point  $d$

$$Pro = d + \frac{2r}{5d}$$

in a second perpendicular

$$d = 39 + \frac{2}{195} = 39 + \frac{1}{92.5} \text{ of an}$$

inch from the center of the Ball

This difference will cause a deflection  
only of  $\frac{1}{10}$  <sup>about</sup> in 2 hours.

3. Feb 1796

Hardness, Softness, Elasticity,  
and fluidity —

A body perfectly hard is that  
whose parts cannot be changed  
as to situation. — Particles separated  
by fire — Phil: a part that the  
constituent particles of all bodies  
must be perfectly hard, this is a  
hasty conclusion. The various app:  
may be accounted for by the change  
of the laws of nature —

Two kinds of hardness, 1. A resistance  
not to change of figure, 2. A resistance  
to a separation of parts. Example  
of iron and hardened steel —

Soft bodies are such whose parts  
separate, or whose position changes  
with the least force impressed.

Soft bodies are divisible, and fluid.

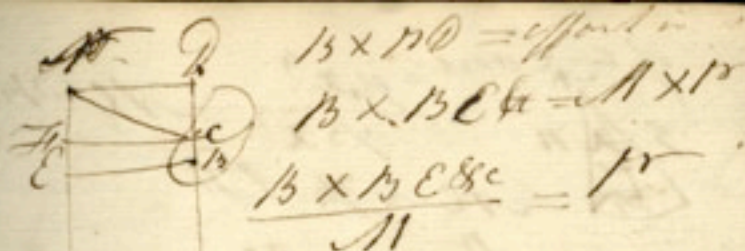
If a body is neither perfectly hard  
nor soft, but requires a continued  
application of power to change its  
figure, it is said to be elastic  
or springy — no body perfectly so  
by the laws of nature. Ivory, <sup>as 12 to 15</sup> next  
hardest that exists. In perfectly  
Elastic bodies will not always  
recover their figure — a piece of wood  
undoubtedly bent will recover its  
position nearly, but bent further

Monday 5 Feb 1776

No lecture this day - Professor  
indisposed - - - - -

Tuesday 6 Feb 1776

Noth<sup>o</sup> a state of Equ<sup>o</sup> of spirit  
the Body - M<sup>o</sup> ought to be in  
stand in working state - but in  
this case - - - - -  
as the subject of Mechanics  
concerned as sufficient to do  
of Hyd<sup>o</sup>; Hydraul<sup>o</sup>; of Trans<sup>o</sup> -  
Gravity is supposed to act in  
parallel lines



$$13 \times 170 = \text{effort}$$

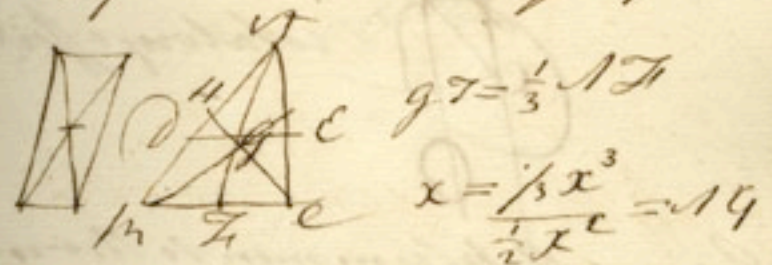
$$13 \times 13 \text{ etc} = M \times 17$$

$$\frac{13 \times 13 \text{ etc}}{M} = 17$$

Center of gravity by C  
not the same with the center  
of the body the bodies  
if near the earth

But this is not sensible in  
the bodies we can see there  
any experiment on it

To find the center of G<sup>o</sup>

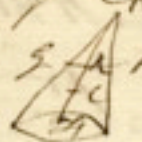


$$gT = \frac{1}{3} AT$$

$$x = \frac{1}{2} x^3 = 19$$

$$\frac{1}{2} x = 19 \text{ etc } 19 = \frac{1}{2} x = 17$$

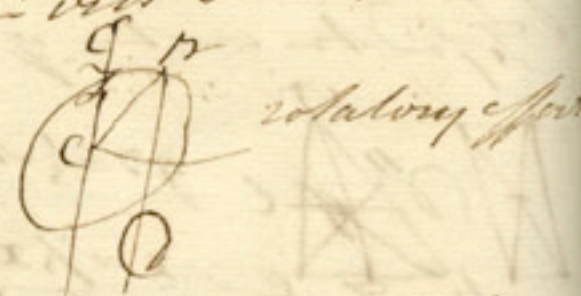
of a Cone  $\frac{1}{2} \pi r^2 h = AC = \frac{3}{4} \pi r^2 h$



$AC = \frac{3}{4} \pi r^2 h$

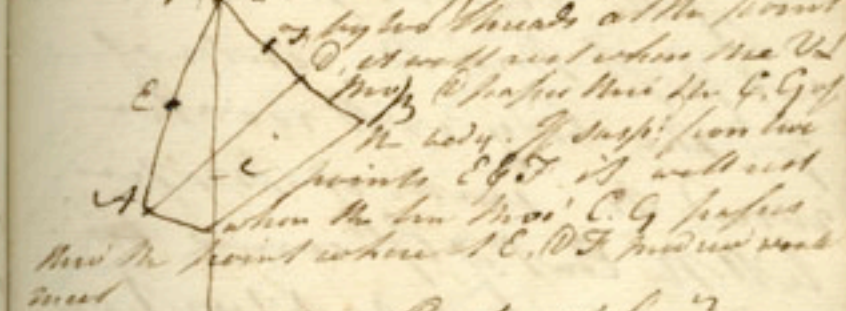
when a line paper  
 C is the center of  
 motion of G!!

there will be no motion  
 But if the V.L. does not pass  
 thro the center of M<sup>o</sup>  
 G<sup>n</sup> there will be a motion



From all experiments there  
 ever ingather will be in the  
 position of Gravity: there  
 offers another method of  
 finding the center of Gravity

also  
 This may be found  
 by laying the body on a table  
 the line V.L. passing thro the  
 center of G<sup>n</sup>



To find the Cent<sup>r</sup> of G<sup>n</sup>  
 multiply all the

7<sup>th</sup> Feb. 1776

A. P. suspending of the Cent. of Gravity  
When the Center of G<sup>ty</sup> is susp.  
the body will be at rest

If the Virtual plane does  
not pass thro' the center of  
G<sup>ty</sup> the body will revolve  
round the center of Motion  
till the Cent. of G<sup>ty</sup> comes to  
underneath of support or  
in a v. line

Ex. A triangle suspended  
as above. with such that  
the center of Gravity is  $\frac{2}{3}$  of  
the height of the base &c as  
shown in last Lecture.

The triangle may be susp.  
at the top or some point

3. A. P. of the C. G. is the  
where the Center of G<sup>ty</sup> coincides  
with the center of M<sup>ty</sup> the body  
will rest in every position.

Any body upon a plane will  
not rest unless the vertical  
passing thro' the C. G. is <sup>the vertical</sup>  
perpendicular to the plane

If the body will always rest  
with the Vertical line thro'  
the C. G. passes thro' resting  
the base. - when it touches the

Plane in two points - axis  
of - it rests but not stable  
When the C. G. falls above

the center of the Eye we can  
it will not rest - but consider  
it with an egg will not rest  
on one end, but will fall off shell

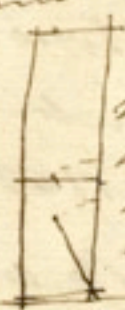
A body moves a little way out  
of its place & returns back to form - not  
with the C.G. ascends. when  
it gets beyond the vertical line  
the body will fall



Prise towers

130 feet high 15 feet base  
Bot: 170 feet high 9 feet base  
Some tall bodies are

more easily pushed down than  
short ones

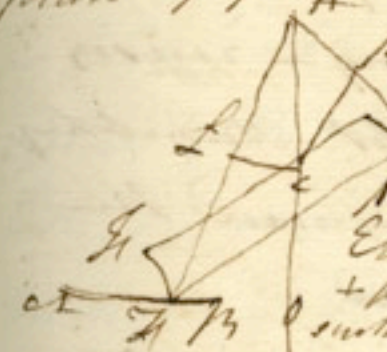


Ex: A cant loaded with heavy  
instruments will give on  
a great quantity -  
then when loaded with  
less weight it may be

no body will rest on an incl:  
plane if there was no friction,  
was this the case even a ball  
would slide down an incl. plane

Body slide down an incl. plane  
when the C.G. falls within  
the points of support - it will  
when it falls without

If a body rest upon one  
incl. plane it will not rest  
till a force per each of the  
planes prevents it in the Vert.



If the line F.H. G.H.  
are drawn perpendicular  
to the points of support  
then the V. line  
is drawn in the V. line  
the C.G. of the  
beam, then the beam  
will rest and if the  
lines C.L, C.R are drawn  
+ per the C.G. C. each pt.  
sustains a pressure :: H.L, H.R

Ex: how much each  
plane supports it is as  
H.L to H.R

Ex: M: of beam joined by  
a small line at the V. point C.G.  
if it is within the points of support  
it will remain ~~where it is~~  
at rest

8 Feb. 1776



A scaffold for  
reparing Mr. Ch. of S. 1<sup>st</sup> room

C.G. in Animal bodies -  
standing - walking -  
waiting - sitting - rising -  
carrying a weight - stretching  
leaping or running round the  
body have inward

Sometimes the center of G.<sup>ty</sup>  
seems to ascend light bodies  
in water - this owing to an  
cause - Double cone will  
with with up or down as the angle  
is great or small

M.M.<sup>n</sup> is an instrument used  
for transferring the action of the  
force to the weight. - commonly  
refined into instruments without  
loss of the power, but this  
is not always the case as  
in Clocks &c. Mech.<sup>n</sup> is the  
sum of the actions - Geometric  
like Dynamics the sum of  
motions - Mech.<sup>n</sup> to be perfect  
give a resistance to the Motion  
powers - Gravity commonly  
overbalanced for the moving  
and the balance of the weight  
M.<sup>n</sup> with simple Com or other  
mediate



Find the Power in the Coords,  
Levers, and Inclined Planes  
of the Lever

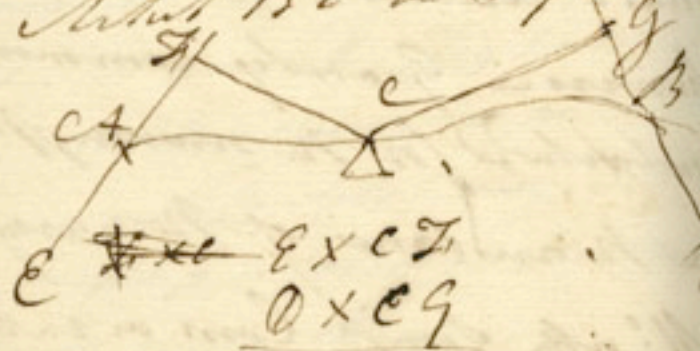
There is any number of  
of any shape moved in  
an instant round a prop

I. Power is when the prop  
is in the middle point

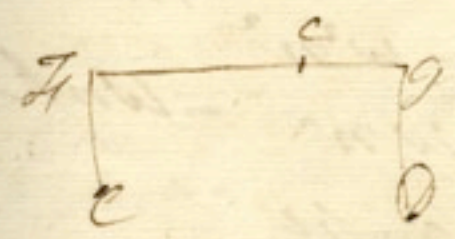
II. Weight is the middle pt

III. Power is the middle pt

Properties of the Lever are:  
for Archib. 152 in Dynamics



Each part as if applied to  
the axis at the center. We  
may substitute any other  
lines equal to the first. Hence  
we may convert the above  
to a straight one



is indifferent when the weight  
is attached whether at F, G  
or at E, D.

- Things to be considered  
in the use of the Lever
- I. Length of the Lever
  - II. V<sup>o</sup> of the weight
  - III. Work performed, or momentum

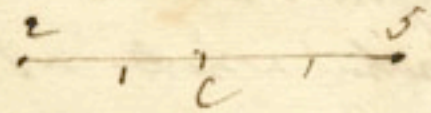
M. - Out of the power  
 W - Out of the weight

$$1. \frac{Pm - Wm}{Pm^2 + Wm^2} = \text{Ang. Velocity}$$

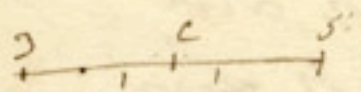
$$2. \frac{PmW - Wm^2}{Pm^2 + Wm^2} = \text{Vel of } W$$

$$3. \frac{PmWm - Wm^2}{Pm^2 + Wm^2} = \text{Work}$$

Example



$$\frac{5 \times 2 - 2 \times 1 = 8}{5 \times 1 + 2 \times 1 = 7} \text{ work done by } M \text{ on } m$$



$$3 \times 1 - 2 \times 1 = \frac{2}{5} \text{ Ang. Vel.}$$

$$3 \times 1^2 + 2 \times 1^2 = 5 \times 1 = 5 \times \frac{2}{5} = 2$$

$$1 \frac{5}{6} \times 1 - 1 = \frac{4}{6} \times 1 = \frac{4}{6}$$

Greater quantity of work done in  
 less time when the weight is  $\frac{2}{5}$  of  
 the power employed. Hence it  
 is not true that the power gains  
 in time lost.

1. Given the proportions of  
 the parts of the machine  
 to find the power to the  
 weight

$$M^2 - 2M^2W - W^2 = 0$$

$$M^2 = W^2 + 2M^2W$$

$$W^2 + 2M^2W = M^4$$

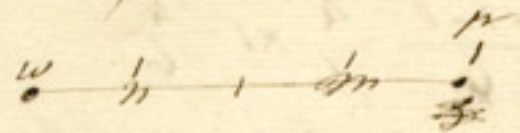
$$W^2 + 2M^2W + M^4 = M^4 + 2M^2W + W^2$$

$$W + M^2 = \sqrt{M^2 + M^4}$$

$$W = \sqrt{M^2 + M^4} - M^2$$

Eq.

9<sup>th</sup> Feb. 1776



$$W = \sqrt{m^2 + m^2} - m^2$$

$$\sqrt{p^2 + 1} - 1$$

$$\sqrt{1 + 1} - 1$$

$$\sqrt{2} = 1.4142$$

$$\frac{1}{1.4142}$$

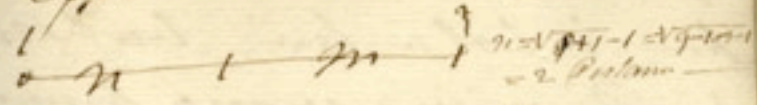
11- Given the power and W  
 to find the proportions of  
 the ~~machine~~ arms of the  
 Lever

$$\frac{P \times n - P \times m^2}{P \times n^2 + W \times n} = \frac{P \times m^2}{P \times n^2}$$

By the this proof the  
 result will be

$$n = \sqrt{p+1} - 1$$

Eq.

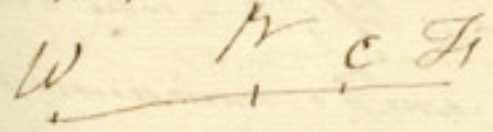


$$p+1 = \sqrt{4} - 1 = 1$$

that is of the power is 3 and  
 the wt. 1 the prop. must be  
 in the middle to produce the  
 most work  
 $\frac{1}{2+1} \& \sqrt{4-1} = 2$

Another case

in equilibrium



$$\frac{L \times F \times p - W \times W \times p}{L \times L \times p^2 + W \times W \times p^2} = R \times L$$

$$L:W::Wp:Lp$$

In the Lever what is gained in  
 power is lost in time, but this  
 proceeds upon a wrong principle  
 for it supposes the power suffi-  
 ce to move the weight w<sup>m</sup> it is  
 only applied to balance the  
 weight.

This however has its ad-  
 vantages in carpentry &c  
 when the machine is in equilib-  
 rium statics — If the power  
 gained is 10 lbs for 1 lb  
 the power would communicate  
 to the weight but half the time  
 the weight would descend it.

Saturday 10<sup>th</sup> Fe 1776

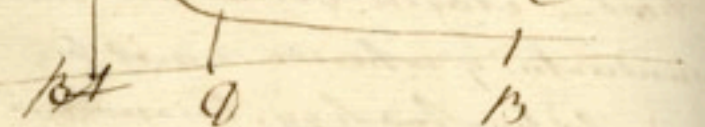
— of Cohesion —

hard — elastic bodies — are  
 conducted by cohesion must be  
 conducted by analogy, because we  
 cannot see the particles in contact  
 — At an infinitely small distance  
 the attraction of G<sup>m</sup> will be infinitely  
 great — Musket Ball —

The Attraction of Dc  
 $\frac{1}{r^2} \times F = 1$   
 $w = AC$   
 A. — 102 — B — C — E

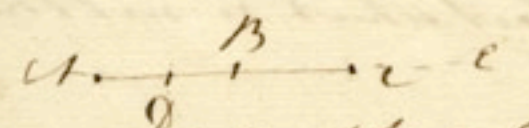
I J N suppose the particles  
 in contact what is not the  
 case

Body moving from B to A all the way at a speed an impulse velocity what. Ev. about C



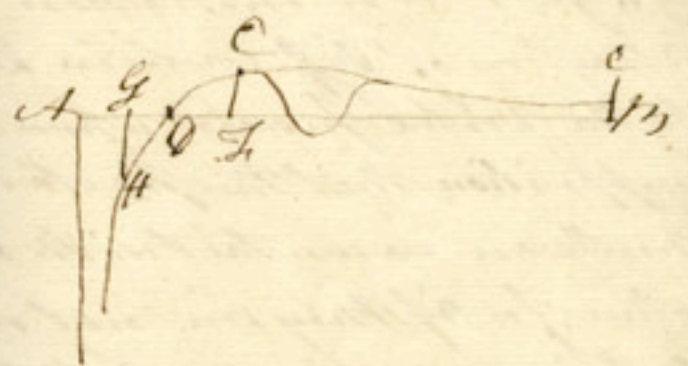
By impulse Vel.<sup>n</sup> we mean a body describing an impulse space in a finite time. Here it appears that it is about to suppose that G<sup>n</sup> can increase as the D<sup>n</sup> ad infinitum. It was probably that the part of matter was not in contact here though the mean

Demonstrated

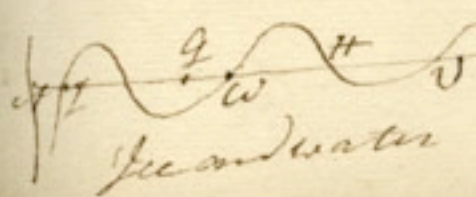


The particles will be in C and E at the same time. 2 & 3 of the particles of matter are in contact

Since we cannot bring particles into contact the at steady in G<sup>n</sup> vanishes.



The greatest pressure cannot bring the particles of bodies into cohesion - two pieces of steel - here two particles of steel are in the common boundary of the attraction and repulsion.



Ice and water

The Power of Gravity does not  
increase accurately: & therefore there  
may be no sensible variation in  
the great bodies of the System.

In J. N. Demonstration of the  
Attraction of Diff. Circles in a cone  
to the Vertex proceeds upon the  
supposition that the particles of  
matter are in contact with each  
other, for if they are not in con-  
tact, his conclusions will by no  
means follow. Many Experiments  
in Electricity, Magnetism & Optics  
show that the particles of matter  
cannot be in contact.

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