

No 2
Reads of a course of Lectures
on Natural Philosophy

— Friday 10th Oct^r 1793

Power

By J. D. Inverness

— Repulsion —

Protein powdered particles will not agar
cohere — Oil and water — water under
dry glass — Needle swims on water — flies
walk on the surface of water with ease but
are immediately attracted and made fast
to brack —

— Gravitation —

If a body is supported it presses up
from its support, if the support be removed
it descends towards the earth — Descend
in time perpendicular to the surface — The
same on all sides of the earth — This is
owing to the attraction of the earth, and
that attraction is called gravitation —
— extends to the greatest heights we can
reach without any sensible diminution —
— Attraction of mountains proved by the
deflection of the plummet in Peru, and
on Schickallen —
— Bodies descend in the same times what
ever be the differences in bulk figure &c. —
— proved by the G. and F. Experiments —
— resistance of the air occasions some diff.
in the descent of bodies — lightest moving
slowest —
— weight of bodies greatest at the surface of
the earth — Decreases inversely as the square
of the distance — Demonstration —
— Below the surface & from the center —

In computing the proportional gravities
of bodies the Distances must be taken for
the centers — Throughout all Distances
to which we have access by Experiment
the gravity will be the same as at the
surface —

— Were the earth a sphere and at rest the
weight of bodies would be the same on all
parts — but as neither is true — Gravity is
diminished at the Equator — Experiments
Pendulums vibrate slower at the Equator
than at a distance from —

— Were the earth a sphere the diminution
of gravity arising from the centrifugal force
will be as the square of the cosine of the latitude —
Demonstration —

— Diminution of Gravity observed by Bou-
guer and Condamine on the Andes —

— Were the earth a hollow shell and
Gravity to act $\frac{1}{2}$ than a particle of mat-
ter would remain any where in this sphere
at rest —

Descent of bodies by Gravity

In perpendicular lines

A body moved by gravity alone has a motion uniformly accelerated

~~Spaces are as the Velocities~~

Spaces are as the velocities

Spaces are as the times — Therefore

Spaces are as the squares of the Velocities or times — Demonstrated from Numbers

from Geometry — Triangle —

The velocity at any given instant is such as if continued uniform would enable the body to describe twice the space from the beginning of the motion

Application —

— To find the Height of an Object from the time of a body's falling from its top. —

— To find the time and Velocity of a body falling below the surface —

+ A body falls in the first second of time

16.1 — From this it shows may be calculated

Spaces described in successive times are as the numbers 1. 3. 5. 7. 9 &c — Odd numbers —

- A body projected upwards is uniformly retarded - follows the same laws as a body uniformly accelerated - The ascending and descending velocity at any given point ^{are} the same -

Figure of the earth the consequence of its attraction -

All the bodies on or connected with the earth are heavy - Air - Smoke - Exhalations - even light itself all are subject to the universal principle of matter -

- It reaches to the moon which is attracted to the earth by this power of attraction & the earth - The planets to the Sun, and the satellites to their primaries -

Descent of Bodies by Gravity

— On inclined planes — ^{fixed}

Motion uniformly accelerated — All motion
velocity the same, as what would have been
acquired in falling thro' the perpendicular
height — The velocities are as the times

— The velocities and time are as the square
roots of the lengths of the plane — Time of

descent on any inclined plane is to the time
of perfect descent, as the length of the plane
to its height — Times on different planes

of the same height are as their lengths

The velocities on inclined planes of different
lengths are as the square roots of their heights

+ The time of descent through any number of
inclined planes connected together is equal

to that through one plain joining their
extremities — Descent through all the chords

of a circle and the Diameter in the same

time — If from any point of the perpen-

dicular height a straight line be drawn at
right angled angles to the inclined plane — The

extreme points of this line will show the correspon-

my places of two bodies one moving along
the inclined plane the other perpendicular
in the same time
Let a sphere roll, and a plane surface slide
down an incl. plane without friction, the spaces
described in the same time from quiescence will be
as 5 to 7
A body falling from the same height acquires the same
velocity whether it descends per. or on any inclined plane.

~~pendulum~~

— Conclusions —

- Vibratio Oscillativa - point of suspension
- cause of pendulum's motion exactly
- Descent from greatest elongation to the point performed in the same time that a body would take to fall through ^{twice} the length of the pendulum or diam. of the circle of which the pendulum is the radius -
- Pendulums of the same length vibrate in the same time, whatever be the proportion of their weights -
- Were the vibrations performed in the chords, great and small would be performed in the same time
- velocity at the lowest point is as the chord of the arc through which it descends -
- Motions in small arcs differ very little from the motions performed in ^{chords} arcs - nearly equal
- Times of vibration in small arcs nearly equal
- Times of oscillation in the subduplicate proportion of their ^{2, 3, or} lengths - Examples -
- Rod pendulum Center of Oscillation at $\frac{2}{3}$ from the point of suspension - center of percussion in a ball of metal suspended by a string the center of Osc. is very near the center of the ball - The Difference is a common Royal pendulum
- At the Equator Vibratio slower - brought to length would gain $139'' = 2' 19''$ in 24 hours - and must be short 72.1262 inch to bring it to time

A pendulum moving in a cycloid per-
forms all its vibrations great and small
Principle properties of the Cycloid - The above
property of the Cycloid supposes all the matter
of the pendulum collected in one point which
is impossible in practice. In a cycloid the Center
of Oscillation is continually changing - Hence
of no use in practice -

Pendulum the best Standard hitherto dis-
covered for weights and Measures -

Principal use of the pendulum is its ap-
plication to clock work -

Compound pendulum - two balls on one
rod, the upper tends to accelerate the motion
of the ~~the~~ lower and the lower to retard that
of the upper -

Projectiles

- A body projected in every direction except that of the perpendicular describes a curve - By the projectile force it would move uniformly in a straight line, describing spaces proportional to the time - By Gravity it is drawn downwards and falls thro' spaces which are as the squares of the time, but a curve which has its abscissa as the square of the corresponding ordinate is a parabola - Every projectile thro' a diameter a parallel Impetus is the perpendicular height thro' which a body must fall to acquire the initial velocity of the projectile -
- The Amplitude or horizontal range is double the impetus - Elev. 45°
- Vertical R. at 45° the greatest -
- Ranges at equal Distances above and below 45° are equal - None any object at Distance less than the greatest range may be hit by two elevations -
- Problems in Gunnery -
- Resistance of the air -

Central Forces

- Planet's motion - Involvement
- Centripetal - Centrifugal forces -
- Table - Slings -
- Projectile force along the Tangent - uniform
- Centripetal force continual pressure towards a point - Center of forces -
- Description of a Circle - Ellipse & by the projectile and Centripetal forces -

Propositions

1. Centripetal forces are \propto quantities of matter in the revolving bodies
2. Centripetal force in a circle would generate the same velocity as that of a body falling thro' half the radius -
3. Centripetal Forces \propto Distances doubly
4. \propto squares of the Period
times reciprocally
5. - Sweep equal areas in equal time
6. Periods times squared are as the Distances - This discovered by Kepler to obtain in the Planetary system -

7. If the centripetal force be different at different distances from the center, then the projectile may describe an ellipse or any other conic section. — In this case
8. Velocities in every point of the orbit will be to each other inversely as perpendiculars to the tangents at those points.
9. In an Elliptical orbit the Force is ^{Centripetal} inversely proportional to the square of the distance. —

These propositions Demons^{tr}ated Geom^{et}rically and illustrated by Experiments on the whirling machine — Circular pendulum &c. —

Collisions

- of inelastic bodies - Balls of putty or clay
 - of Elastic bodies - wavy balls
 - Direct and oblique impact
- Propositions

* - vide Newtons two general propositions
which include all the Phenomena
- also Hamiltons 4th Lecture - Parkin-
son on impact

Doctrine of infinitesimals

- Terms and relations of various Extensive
- Fluxions - nature and application of
each